Astrometry with ground-based interferometers

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Abstract. We review the status of ground-based interferometric astrometry. This will include a review of technology and results in differential techniques (e.g. relative orbit determination), as well as global astrometry techniques (globally-registered parallax and proper-motion estimates).

Keywords. instrumentation: interferometers, techniques: high angular resolution, techniques: interferometric, astrometry, binaries: general

1. Introduction

In this contribution we review the status on long-baseline (LB) optical/near-IR (OIR) interferometric astrometry. Operationally we define a long-baseline interferometer as a device that combines light from multiple independent telescopes to form and measure interference *fringes* – variations in detected power as a function of optical path difference between two telescopes. This definition excludes our consideration of interferometry using a single telescope aperture (e.g. "speckle" or aperture masking interferometry). And as the title implies we will discuss interferometric astrometry in the optical and near-IR; the many contributions and future potential of interferometric astrometry in radio and mm bands are discussed in other contributions to these proceedings (e.g. see manuscripts by Reid, Lestrade, and Loinard).

An astronomical interferometer is a device that measures interference (or attributes associated with the interference) in the incident radiation field from an astronomical source. This first such interferometer operating in OIR bands was constructed by Michelson at Mt. Wilson in 1920. The astrometric potential of LB OIR interferometers was appreciated by Michelson (1920) in their development; Anderson (1920) and Merrill (1922) observed a number of binary stars with the Michelson's Mt. Wilson interferometer, and published the first estimates of Capella's visual orbit. Since that time until today LB OIR interferometers have been used extensively in relative astrometry of stars over fields from milliarcseconds to tens of degrees, and when combined with external, global reference frames (e.g. FK5 or Hipparcos) such measurements have been used to compute differential corrections to stellar positions, with hopes of extending these analyses to globally-registered proper motion and parallax estimates.

In what follows we will survey astrometric methods used with LB OIR interferometers, and survey the scientific contributions made with these techniques.

2. Astrometric methods with interferometers

LB OIR interferometers perform astrometry of stellar fields by analyzing the *fringe* patterns of stars measured by the interferometer. (The reader unfamiliar with astronom-

ical interferometry and interferometric observables is referred to Perley *et al.* 1989, Shao & Colavita 1992b, Thompson *et al.* 2001, Quirrenbach 2001, and Boden 1999a).

Depending on the parameters of the stellar field and the interferometer, the exact analysis methods can be different, but generally all methods fall into two broad classes:

• Fringe amplitude Astrometry: When the fringe patterns from multiple sources overlap (i.e. are within a fringe coherence length), the (power-normalized) fringe amplitude contains information on the relative separation and brightness of the sources. Fringe amplitude analysis necessarily applies when multiple sources are within a coherence length of each other, so this technique is applicable only over very small astrometric fields – field sizes of millarcseconds to on the order of 100 millarcseconds (depending on interferometer parameters). With such field sizes these amplitude techniques have typically been used in the resolution and orbital analysis of close binary stars. Notable in fringe amplitude analysis is the necessity to include the relative brightness between the sources in the astrometric analysis.

• Separated fringe packet astrometry: When fringe patterns from multiple sources are well separated (i.e. by multiple coherence lengths) in delay space, then the delay separation between fringe packets contains information on the relative separation of the sources. For fields larger than about 100 millarcseconds the separation between multiple fringe packets in delay space is the observable proxy for sky separation. Operationally various observation and measurement techniques are applied as a function of field size, but the common thread is the delay separation between objects in the field.

3. Visibility amplitude results

The first and largest body of scientific results from LB OIR interferometric astrometry follow from visibility amplitude analysis of close binary stars. As mentioned above, such binary star analysis was initially described by Michelson himself (1920), and using his interferometer Anderson (1920) and Merrill (1922) observed a number of binary stars, and published the first orbit determinations for the Capella system. The visibility amplitude effects created by the overlap of multiple fringe packets within a single coherence length are straightforward to compute (see Michelson 1920 and Boden 1999a). Astrometry using this method began with Capella, but has been broadly applied with contributions from most ground-based LB OIR interferometers (e.g. Table 1). Figure 1 illustrates a visual orbit on the nearby binary ι Pegasi (Boden *et al.* 1999b) reconstructed from interferometric visibility data from the Palomar Testbed Interferometer (PTI; Colavita et al. 1999). Interferometric visibility measurements serve as proxy for relative astrometry between the components, allowing an estimate of the component separation (and over time the orbit). Modern visibility analysis methods estimate the orbit directly from the visibility data without intermediate separation estimates (e.g. Herbison-Evans 1971 and Hummel 1993), and directly integrate radial-velocity (RV) data when available (e.g. Hummel 1998) and Boden 1999c).

The primary objective in most visibility amplitude/binary analyses is the determination of fundamental parameters (e.g. dynamical mass, radius, luminosity) for the components (a notable exception is work on Atlas by Pan *et al.* 2004 and Zwahlen *et al.* 2004 discussed elsewhere in these proceedings). Table 1 (reprinted from Cunha *et al.* 2007) lists the set of binary systems that have been analyzed using LB OIR interferometric data combined with double-lined RV data. There are a total of 34 systems listed spanning nearly the entire HR-diagram; all but three of these entries (discussed below) use interferometric visibility data as proxy for the component astrometry. Notable in this list are contributions on open cluster stars (e.g. θ^2 Tau; Armstrong *et al.* 2006), pre-main

Table 1. Interferometrically determined orbits and component masses for double-lined spectroscopic binaries. More details are available in the references listed below the table. The star κ Peg is a triple system; in this case the "wide" (A – Ba/Bb) and "narrow" (Ba – Bb) orbits are listed separately. Reprinted with permission from Cunha *et al.* (2007).

System	Spectral Types	$a^{\prime\prime}$ [mas]	$M_1 \ [M_{\odot}]$	$M_2 \ [M_{\odot}]$	Instr.	Ref.
HD 27483	F6V + F6V	1.3	1.38 ± 0.13	1.39 ± 0.13	PTI	K04
α Vir	B1III-IV+B3V:	1.5	10.9 ± 0.9	6.8 ± 0.7	Narrabri	H71
κ Peg B	F5IV + K0V:	2.5	1.662 ± 0.064	0.814 ± 0.046	PTI	M06
V773 Tau A	K2+?	2.8	1.54 ± 0.14	1.332 ± 0.097	KI	B07
θ Aql	B9.5III + B9.5III	3.2	3.6 ± 0.8	2.9 ± 0.6	MkIII	H95
β Aur	A2V + A2V	3.3	2.41 ± 0.03	2.32 ± 0.03	MkIII	H95
12 Boo	F9IV + F9IV	3.4	1.435 ± 0.023	1.408 ± 0.020	PTI	B00
		3.5	1.416 ± 0.005	1.374 ± 0.005	combined	B05b
σ Sco	B1III+B1V	3.6	18.4 ± 5.4	11.9 ± 3.1	SUSI	N07b
γ^2 Vel	O7.5II + WC8	3.6	28.5 ± 1.1	9.0 ± 0.6	SUSI	N07c
BY Dra	K4V + K7.5V	4.4	0.59 ± 0.14	0.52 ± 0.13	PTI	B01
o Leo	F9 + A5m	4.5	2.12 ± 0.01	1.87 ± 0.01	combined	H01
HD 9939	K1IV + K0V	4.9	1.072 ± 0.014	$0.838 {\pm} 0.008$	PTI	B06
σ Psc	B9.5V + B9.5V	5.6	2.65 ± 0.27	2.36 ± 0.24	PTI	K04
64 Psc	F8V+F8V	6.5	1.223 ± 0.021	1.170 ± 0.018	PTI	B99c
93 Leo	G5III + A7V	7.5	2.25 ± 0.29	1.97 ± 0.15	MkIII	H95
ζ^1 UMa	A2V + A2V	9.6	2.51 ± 0.08	2.55 ± 0.07	MkIII	H95
		9.8	2.43 ± 0.07	2.50 ± 0.07	NPOI	H98
ι Peg	F5V+G8V	10.3	1.326 ± 0.016	0.819 ± 0.009	PTI	B99b
η And	G8III+G8III	10.4	2.59 ± 0.30	2.34 ± 0.22	MkIII	H93
α Equ	G2III+A5V	12.0	2.13 ± 0.29	1.86 ± 0.21	MkIII	A92b
27 Tau	B8III+?	13.1	4.74 ± 0.25	3.42 ± 0.25	combined	Z04
$HD\ 195987$	G9V+?	15.4	0.844 ± 0.018	$0.665 {\pm} 0.008$	PTI	T02
ζ Aur	K4Ib+B5V	16.2	5.8 ± 0.2	4.8 ± 0.2	MkIII	B96
θ^2 Tau	A7III+A:	18.6	2.1 ± 0.3	1.6 ± 0.2	MkIII	T95
		18.8	2.15 ± 0.12	1.87 ± 0.11	combined	A06
λ Vir	Am + Am	19.8	1.897 ± 0.016	1.721 ± 0.023	IOTA	Z07
HD 98800 B	K5V+?	23.3	0.699 ± 0.064	0.582 ± 0.051	KI	B05a
ϕ Cyg	K0III+K0III	23.7	$2.536 {\pm} 0.086$	2.437 ± 0.082	MkIII	A92a
α And	B8IV + A:	25.2	5.5:	2.3:	MkIII	P92, T95
β Cen	B1III+B1III	25.3	11.2 ± 0.7	9.8 ± 0.7	SUSI	D05,Au06
β Ari	A5V+G0V:	36.1	2.34 ± 0.10	1.34 ± 0.07	MkIII	P90
λ Sco	B1.5IV + B2V	49.3	10.4 ± 1.3	8.1 ± 1.0	SUSI	T06
12 Per	F8V+G2V	53.2	$1.382 {\pm} 0.019$	1.240 ± 0.017	CHARA	Ba06
α Aur	G1III+G8III	55.7	2.56 ± 0.04	2.69 ± 0.06	MkIII	H94
δ Equ	F7V + F7V	231.9	1.193 ± 0.012	1.188 ± 0.012	PTI	M05
κ Peg	F5IV + F5IV	235.0	1.549 ± 0.050	$\operatorname{composite}$	PTI	M06

References: A92a: Armstrong 1992a; A92b: Armstrong 1992b; A06: Armstrong 2006; Au06: Ausseloos 2006; Ba06: Bagnuolo 2006; B96: Bennett 1996; B99b: Boden 1999b; B99c: Boden 1999c; B00: Boden 2000; B01: Boden & Lane 2001; B05a: Boden 2005a; B05b: Boden 2005b; B06: Boden 2006; B07: Boden 2007; D05: Davis 2005; H71: Herbison-Evans 1971; H93: Hummel 1993; H94: Hummel 1994a; H95: Hummel 1995; H98: Hummel 1998; H01: Hummel 2001; K04: Konacki & Lane 2004; M05: Muterspaugh 2005; M06: Muterspaugh 2006; N07a: North 2007a; N07b: North 2007b; P90: Pan 1990; P92: Pan 1992; T95: Tomkin 1995; T02: Torres 2002; T06: Tango 2006; Z04: Zwahlen 2006; Z07: Zhao 2007

sequence stars (e.g. V773 Tau; Boden *et al.* 2007), low-abundance/Galactic thick-disk stars (e.g. HD 195987; Torres *et al.* 2002), subgiant (e.g. 12 Boo; Boden *et al.* 2005b) and giant (e.g. α Equ; Armstrong *et al.* 1992b) stars, and even triple systems (η Vir; Hummel *et al.* 2003). Prospects are excellent for continued important contributions in these areas.



Figure 1. Visual Orbit of ι Pegasi and Supporting Visibility Data (from Boden (1999b)). Top: the relative visual orbit of ι Pegasi, with the primary rendered at the center, and the secondary position shown at both maximum elongation and conjunction. The ι Peg orbit is in fact circular but seen at a near-eclipsing orientation. Bottom: four consecutive nights of PTI calibrated visibility (V²) data on ι Peg. Variations in the measured visibility can be used as proxy for the relative separation between the components.

4. Separated fringe-packet astrometry

Fringe amplitude astrometry techniques necessarily require the multiple sources to be within a single interferometric coherence length, typically on the order of tens to ≈ 100 mas projected on the sky. When astrometric fields increase beyond this 100 mas, multiple fringe packets are well-separated in interferometric delay space, and the delay difference itself becomes the observable proxy for relative astrometry. Above we have described such astrometry as separated fringe packet astrometry.

As a practical matter, separated fringe packet astrometry further subdivides into three different operating regimes that we will discuss in turn.

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4.1. Very narrow angle astrometry

When the astrometric field is still within a interferometer sub-aperture (single telescope) diffraction pattern (e.g. ≈ 1 arcsec), then the multiple fringe packets can be observed simply by scanning the delay compensation device (typically a "delay line"; Colavita *et al.* 1999). By measuring the delay scan distance separating the multiple fringe packets (typically by laser metrology) one obtains an astrometrically-useful delay difference estimate. The first results of this kind are presented in Colavita (1994), and this method is described in detail in Lane & Muterspaugh 2004 (including performance improvements from synthetic phase stability allowed by the unique PTI dual-beam/fringe tracker design). When phase referencing is available typical relative astrometric precisions are on the order of 15 μ arcseconds over a 0.5 arcsecond field (a fractional precision of 3 parts in 10⁵). Astrophysical results from this method are included in the Table 1 compilation: δ Equ (Muterspaugh *et al.* 2005), κ Peg (Muterspaugh *et al.* 2006), and 12 Per (Bagnuolo et al 2006). Further, such astrometric precision enables planet-search programs, and the PTI PHASES astrometric planet search program is discussed in Muterspaugh *et al.* (2006) and Muterspaugh *et al.* (2007)

4.2. Dual-beam narrow-angle astrometry

While astrometric precisions at the arcsecond-scale are remarkable, the small working angles practically dictate that the methods are limited to arcsecond-scale binaries. A method to increase this field to expand sky coverage was presented by Shao & Colavita (1992a). In this narrow-angle astrometric scenario the fringes on multiple stars are tracked simultaneously to take advantage of significant correlation in the atmospheric phase noise over an *isoplanatic angle* (\approx 30-40 arcsec in the near-IR; Quirrenbach 1999). The simultaneous fringe tracking requirement necessitates multiple beam combiners in a single facility, and guided the dual-fringe tracker design of PTI (Colavita *et al.* 1999). Hence this technique has been termed dual-beam narrow-angle astrometry.

This dual-beam astrometric technique has been demonstrated at PTI. Figure 2 shows the results of a three-months demonstration experiment performed in 1999 using the well-studied, nearby visual binary 61 Cygni. 61 Cyg is a nearby K-dwarf binary with an estimated 678-year orbital period and apparent separation at present epoch of roughly 31 arcseconds (Gorshanov et al. 2006). Using the PTI N-S baseline (so the principle measurement axis is in declination) PTI collected narrow-angle astrometric data on 61 Cyg over a three-month period in 1999. These astrometric measurements are made by tracking fringes on the two stars with two independent fringe trackers, and relating the relative delay between the two fringe trackers using a laser metrology system (details are given in Colavita et al. 1999). Projecting the derived 2-d separations into a space of declination vs time, the apparent night-to-night separation increase is clearly seen. Fitting a linear motion model to these separations, the ensemble RMS declination residual is 170 μ arcseconds, with a particularly stable, contiguous 7-night run showing a 100 μ arcseconds scatter around the same ensemble motion model. This scatter represents a fractional precision of 3 parts in 10^6 . Application of this method to ground-based astrometric planet searches is planned for the VLTI PRIMA instrument, discussed in detail elsewhere in these proceedings (e.g. see contributions by Richichi and Launhardt).

4.3. Wide-angle astrometry

The narrow-angle method of Shao & Colavita (1992a) leverages the significant correlation in atmospheric turbulence over an isoplanatic angle (30-50 arcseconds at a typical site) to make 10-100 μ arcseconds-class relative astrometric measurements. For interferometric measurements over a wider field this correlation is not applicable. Such wide-angle



Figure 2. Principle Projection for 1999 PTI Dual-Beam Narrow-Angle Astrometry Demonstration. Roughly three months of relative astrometry data on the 30-arcsecond visual binary 61 Cygni are shown projected onto the principle (declination) measurement axis (all astrometric data was taken with the PTI N-S baseline) vs time. The apparent night-to-night relative motion due to the estimated 678-year orbit period is clear in these data. The apparent relative declination motion of 300 μ arcsecond/day is very close to that measured by the Hipparcos satellite (the difference between the two estimates is consistent with acceleration from the binary orbit). The RMS scatter of these data around the best-fit linear motion model is 170 μ arcsecond; data from a particularly stable 7-night run (inset) shows an RMS scatter of approximately 100 μ arcsecond

measurements have been demonstrated by the Mark III interferometer (Shao *et al.* 1988) and Navy Prototype Optical Interferometer (NPOI; Armstrong *et al.* 1998).

Mark III wide-angle astrometry work is described in Mozurkewich *et al.* (1988), Shao *et al.* (1990), and Hummel *et al.* (1994b). This work focused on making serial delay measurements on a set of roughly 20 FK5 stars over a number of years, and using the data to compute differential corrections to the mean-epoch positions from the FK5 catalog. Shao *et al.* (1990) reports single-season RMS residuals of individual measurements on the order of 10 milliarcseconds, with Hummel *et al.* (1994b) reporting four-year ensemble RMS precisions on the order of 20 milliarcseconds. Over a wide-angle field on the order of 1 radian these measurements represent a fractional single-night precision of 1 part in 10^7 .

Based on the success of Mark III wide-angle program, the NPOI was constructed to allow wide-angle astrometry over an extended period, with the objective of extending the proper-motion time baseline for Hipparcos stars. Benson *et al.* (2004) and Johnston *et al.* (2006) report on NPOI astrometry program status. At present NPOI astrometry is demonstrating 10-millarcsecond-class astrometric measurement precision in single-night runs, and the NPOI team anticipate multi-night ensemble astrometric solutions to be completed in the next year. NPOI wide-angle astrometry holds the promise to significantly improve the precision of Hipparcos proper motion and parallax estimates over the next few years, particularly in advance of Gaia (discussed elsewhere in these proceedings by Lindegren and Mignard).

5. Summary

We have summarized astrometric contributions by LB OIR interferometers. To date the largest body of results have focused on analysis of binary systems with an eye toward stellar fundamental parameter determinations, and interferometers will continue making important contributions in these areas (e.g. see Cunha *et al.* 2007 for a discussion). Further, the VLTI PRIMA facility is planning a broad astrometric exoplanet search program (see other contributions by Richichi and Launhardt in these proceedings); prospects are excellent for this (and other) astrometric survey(s) to contribute to understanding of the architecture and diversity of planetary systems.

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