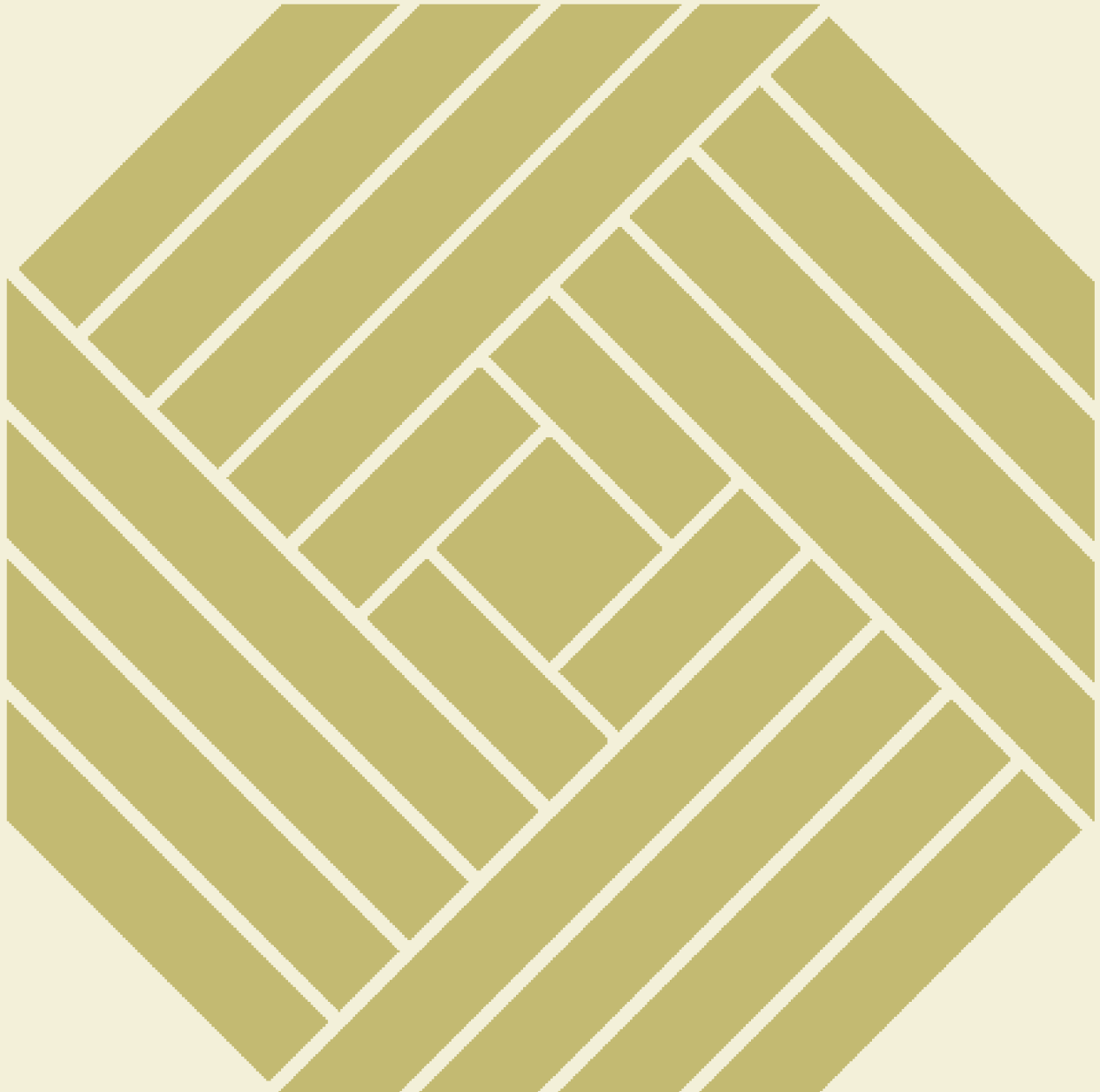


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# COMPOSITIO MATHEMATICA

VOLUME 160 NUMBER 9 SEPTEMBER 2024

- Gebhard Böckle, Tony Feng, Michael Harris, Chandrashekar B. Khare and Jack A. Thorne** Cyclic base change of cuspidal automorphic representations over function fields 1959–2004
- Xin Jin** A Hamiltonian  $\coprod_n BO(n)$ -action, stratified Morse theory and the  $J$ -homomorphism 2005–2099
- Maksim Zhykhovich** The  $J$ -invariant over splitting fields of Tits algebras 2100–2114
- Masaaki Furusawa and Kazuki Morimoto** On the Gross–Prasad conjecture with its refinement for  $(SO(5), SO(2))$  and the generalized Böcherer conjecture 2115–2202
- Sam P. Fisher** Improved algebraic fibrings 2203–2227
- Ronno Das and Sean Howe** Cohomological and motivic inclusion–exclusion 2228–2283