

Beam positioning stability analysis on large laser facilities

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Abstract

Beam positioning stability in a laser-driven inertial confinement fusion (ICF) facility is a vital problem that needs to be fixed. Each laser beam in the facility is transmitted in lots of optics for hundreds of meters, and then targeted in a micro-sized pellet to realize controllable fusion. Any turbulence in the environment in such long-distance propagation would affect the displacement of optics and further result in beam focusing and positioning errors. This study concluded that the errors on each of the optics contributed to the target, and it presents an efficient method of enhancing the beam stability by eliminating errors on error-sensitive optics. Optimizations of the optical system and mechanical supporting structures are also presented.

Keywords: beam stability, beam propagation, sensitivity, laser optics, vibration

1. Introduction

Laser-driven inertial confinement fusion (ICF) is a feasible method to realize controllable fusion, which is expected to be one of the best solutions for the global energy problem^[1]. In a laser-driven ICF facility, several high-power coherent laser beams uniformly focus on a micro-dimension target to generate high-temperature and high-pressure conditions, thereby causing atomic fusion^[2]. Moreover, this method can also be used to explore basic sciences, such as astrophysics phenomena, materials science, nuclear science, and so on.

Each coherent laser beam initially transmits lots of optics for hundreds of meters to enhance its energy and adjust its proper direction to achieve the aforementioned conditions^[3]. A typical diagram of a single laser beam in a laser-driven ICF facility after removing all the mirrors is given in Figure 1. The laser beam is magnified by several spatial filters, and the whole optical system is supported by optical trusses fixed to the base ground. However, a tiny disturbance in the optics would affect the beam stability during its long-distance propagation and high precision. Thus, a laser-driven ICF facility requires extreme high precision. Furthermore, researchers have conducted excellent studies on the experimental environment surrounded by all kinds of vibration disturbances. For instance, Tietbohl *et al.*^[4] analyzed the beam stability caused by mirror supporting systems. Swensen *et al.*^[5] analyzed the errors caused by structural vibration using

the finite element method. Liu *et al.*^[6,7] built a new structural model for analyzing the errors induced by structural vibrations and analyzed the lens vibration sensitivities to the ICF facility targets. Several optics exist in a laser-driven ICF facility; however, the same error on different optics would have different effects on the target, indicating that the error sensitivities to the target would be different with different optics.

This study focused on how the errors of different optics contributed to the target. The errors were mainly caused by vibrations, and thus were regarded as vibration sensitivities. Section 2 describes in detail the vibration sensitivities of the lenses and reflecting mirrors in a laser-driven ICF facility, including their features. In Section 3, we report how the theoretical models in Section 2 were applied to SG-II facilities, and the results that were obtained. Section 4 describes several practical mechanical structure designs to eliminate errors and decrease system errors.

2. Vibration sensitivity models

There are mainly two kinds of vibration-sensitive optics in ICF facilities. One is the focusing lenses and the other is the reflecting mirrors. Previous studies indicated that only the translational movements of the lenses and the rotational disturbances affect the beam direction.

2.1. Models for lenses

A schematic of the lenses for a single beam in laser-driven ICF facilities is shown in Figure 1. The two adjacent

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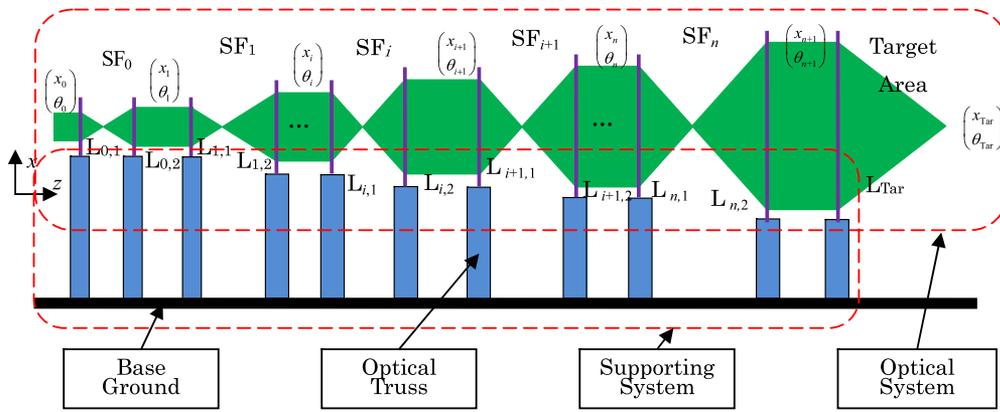


Figure 1. Schematic of a single laser beam in a laser-driven ICF facility without mirrors.

focusing lenses are initially combined to form a spatial filter to adjust the beam quality. Finally, the laser beam reaches the target area and is focused by the targeting lens L_{Tar} after passing through several filters.

The lenses are forced to vibrate because of the disturbances. However, only translational disturbance should be discussed because the rotational vibration is insensitive to the beam direction. For simplicity, the discussion on the vibrating model is based on three hypotheses: the lenses vibrate around their ideal positions, indicating that their average displacements from the required place over time are zero; only the x -direction translational vibration was taken into account without loss of generality; and the targeting lens L_{Tar} was relatively fixed, indicating that no positional error occurred between the two objects.

According to Ref. [7], the relationship between the incident beam into the i th spatial filter (SF_i) and the $(i + 1)$ th spatial filter (SF_{i+1}) satisfies

$$\begin{pmatrix} x_{i+1} \\ \theta_{i+1} \\ 1 \end{pmatrix} = \begin{pmatrix} -m_i & k_i & r_i \\ 0 & -\frac{1}{m_i} & g_i \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x_i \\ \theta_i \\ 1 \end{pmatrix} = [B_i] \begin{pmatrix} x_i \\ \theta_i \\ 1 \end{pmatrix}, \tag{1}$$

$$m_i = \frac{f_{i,2}}{f_{i,1}} = \frac{D_{i,2}}{D_{i,1}}, \tag{2}$$

$$k_i = f_{i,1} + f_{i,2} - \frac{l_i}{m_i}, \tag{3}$$

$$r_i = \left(1 + m_i + \frac{l_i}{f_{i,2}} \right) a_{i,1} - \frac{l_i}{f_{i,2}} a_{i,2}, \tag{4}$$

$$g_i = \frac{a_{i,1} - a_{i,2}}{f_{i,2}}, \tag{5}$$

where x_i and θ_i are the displacement and the angle of incident beam into SF_i , respectively; x_{i+1} and θ_{i+1} are the displacement and the angle of incident beam into SF_{i+1} , respectively; $[B_i]$ is the transfer matrix of SF_i ; $D_{i,1}$ and $D_{i,2}$ are the beam apertures in $L_{i,1}$ and $L_{i,2}$, respectively; m_i is the beam aperture expanding ratio (BAER) in SF_i ; l_i is the distance between the second lens of SF_i ($L_{i,2}$) and the first

lens of SF_{i+1} ($L_{i+1,1}$); $f_{i,1}$ and $f_{i,2}$ are the focal lengths of $L_{i,1}$ and $L_{i,2}$ in SF_i , respectively; and $a_{i,1}$ and $a_{i,2}$ are the x -axis translational displacements of $L_{i,1}$ and $L_{i,2}$, respectively [7].

In the last part, the laser beam was focalized to the target by L_{Tar} , and the transfer matrix $[C]$ from the incident beam into L_{Tar} to the focal plane satisfies

$$[C] = \begin{pmatrix} 0 & f_T & a_T \\ -\frac{1}{f_T} & 1 & \frac{a_T}{f_T} \\ 0 & 0 & 1 \end{pmatrix}, \tag{6}$$

where f_T is the focal length of L_{Tar} and a_T is the vibrating displacement of L_{Tar} .

Supposing $n + 1$ spatial filters are marked from SF_0 to SF_n , and combining Equation (1) to Equation (6), the beam information on the target $(x_{Tar} \ \theta_{Tar})'$ then satisfies

$$\begin{pmatrix} x_{Tar} & \theta_{Tar} & 1 \end{pmatrix}' = [C][B_n] \cdots [B_1] \cdots [B_0] \begin{pmatrix} x_0 & \theta_0 & 1 \end{pmatrix}', \tag{7}$$

where x_0 and θ_0 are the displacement and the angle of the whole optical incident beam, respectively.

Finally, the position of the laser beam focalized in the focal plane x_{Tar} is

$$x_{Tar} = \frac{(-1)^{n+1}}{\prod_{i=0}^n m_i} f_T \theta_0 + \sum_{i=0}^n (-1)^{n-i} q_i (a_{i,1} - a_{i,2}) + a_T, \tag{8}$$

$$q_i = \frac{1}{\prod_{j=i}^{n+1} m_j} \frac{f_T}{f_{i,1}} = \frac{1}{\prod_{j=i+1}^{n+1} m_j} \frac{f_T}{f_{i,2}} = \frac{D_{i,1}}{D_T} \frac{f_T}{f_{i,1}} = \frac{D_{i,2}}{D_T} \frac{f_T}{f_{i,2}}, \tag{9}$$

where D_T is the beam aperture in L_{Tar} . m_{n+1} is set to zero when only $n + 1$ spatial filters exist, to simplify the expression.

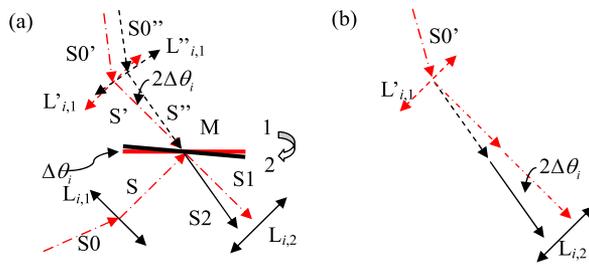


Figure 2. Schematic diagram of a mirror in spatial filter (SF_{*i*}).

The transmissibility error from each vibrating lens to the target was defined as the lens vibration sensitivity (LVS); thus, the following equations were obtained according to Equations (8) and (9):

$$\Delta x_{i,1} = (-1)^{n-i} q_i a_{i,1}(t) = (-1)^{n-i} \frac{D_{i,1}}{D_T} \frac{f_T}{f_{i,1}} a_{i,1}(t), \tag{10}$$

$$\Delta x_{i,2} = (-1)^{n+1-i} q_i a_{i,2}(t) = (-1)^{n+1-i} \frac{D_{i,2}}{D_T} \frac{f_T}{f_{i,2}} a_{i,2}(t). \tag{11}$$

The absolute LVS values of the two lenses in SF_{*i*} were both *q_i*, but they are opposite in direction. Based on Equations (10) and (11), the LVS is:

- (i) proportional to the focal length of the focusing lens,
- (ii) inversely proportional to the focal length of the error lens, and
- (iii) inversely proportional to the BAER from the error lens to the focusing lens.

2.2. Models for mirrors

In ICF facilities, mirrors are widely used to change beam directions. Based on the placement, mirrors are classified into two circumstances: in the first, the mirrors are placed in the spatial filters, and in the second, they are between the spatial filters.

2.2.1. Mirrors in spatial filters

A schematic of a mirror placed in the *i*th spatial filter is given in Figure 2. The reflecting mirror M is placed between L_{*i,1*} and L_{*i,2*} in SF_{*i*}. Ideally, the reflecting mirror M is in state 1, and the central-dashed line S0–S–S1 is the ideal beam path from L_{*i,1*} to L_{*i,2*}. However, for some reason, the reflecting mirror M changed to state 2 with an angle of Δθ_{*i*}, and the real beam path was changed to S0–S–S2, marked with the solid line after the reflecting mirror M. By calculation, the emergent beam was deflected by 2Δθ_{*i*}. The equivalent schematic is shown in Figure 2b.

Supposing the beam deflection was generated by the deviation of L_{*i,1*}, the deviation of L_{*i,1*} was calculated as 2Δθ_{*i*}/f_{*i,1*} [8]. In other words, the error effect of the reflecting mirror in SF_{*i*} to the target with an angular deflection of Δθ_{*i*}

was equivalent to the error generated by L_{*i*} in SF_{*i*}, with a translational deviation of 2Δθ_{*i*}f_{*i,1*}.

Based on Equation (10), the error in the target Δx_{*i*} generated by the reflecting mirror in SF_{*i*}, with deflection of Δθ_{*i*} is

$$\Delta x_{1i} = (-1)^{n-i} p_{1i} \Delta \theta_i, \tag{12}$$

$$p_{1i} = \frac{2f_T}{n+1} = 2f_T \frac{D_{i,1}}{D_T} \prod_{j=i} m_j, \tag{13}$$

where *p_{1i}* is regarded as the mirror vibration sensitivity (MVS) of the reflecting mirrors in SF_{*i*}, since the MVS represents the transmissibility error from the reflecting mirror to the target.

2.2.2. Mirrors between spatial filters

Supposing the mirror is placed between SF_{*i-1*} and SF_{*i*}, similar to the mirrors in spatial filters, the lenses in Figure 2 should be replaced, so L_{*i,1*} and L_{*i,2*} are replaced by L_{*i-1,2*} and L_{*i,1*}. Similarly, the error in target Δx_{*2i*} generated by the reflecting mirror between SF_{*i,1*} and SF_{*i*} with deflection of Δθ_{*i*} satisfies

$$\Delta x_{2i} = (-1)^{n-i} p_{2i} \Delta \theta_i, \tag{14}$$

$$p_{2i} = \frac{2f_T}{n+1} = 2f_T \frac{D_{i-1,2}}{D_T} = 2f_T \frac{D_{i,1}}{D_T} \prod_{j=i} m_j, \tag{15}$$

where *p_{2i}* is the MVS of the reflecting mirrors between SF_{*i,1*} and SF_{*i*}.

The MVS values (*p_T*) between the last spatial filter and the target can also be included in this expression by regarding the beam aperture as *D_T*.

2.2.3. Sub-conclusion for MVS

The comparison between Equations (14) and (15) and Equations (12) and (13) shows that the MVS values of the mirrors between the spatial filters were the same as those of the mirrors between the spatial filter and the preceding spatial filter.

The MVS values of the reflecting mirrors in the spatial filters and the reflecting mirrors between the spatial filter and its preceding spatial filter are all expressed as *p_i* to simplify the expression. The subscript *i* represents the *i*th spatial filter, thereby obtaining the following equation:

$$p_i = p_{1i} = p_{2i} = \frac{2f_T}{n+1} = 2f_T \frac{D_{i,1}}{D_T} \prod_{j=i} m_j. \tag{16}$$

Based on Equation (16), the MVS is

- (i) proportional to the focal length of the focusing lens, and

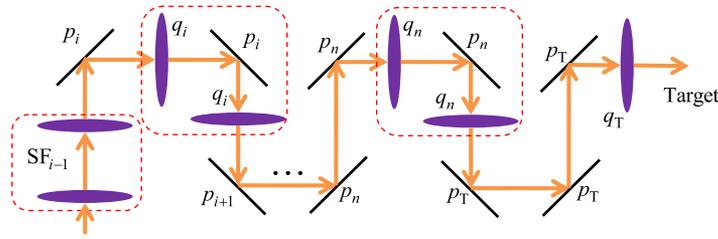


Figure 3. Variance of weighing factors in laser-driven ICF facilities.

Table 1. Optical parameters of SG-II Origin.

Spatial filters	$f_{i,2}$ (m)	m_i	q_i	p_i
SF ₀	1.0	2.000	0.0034	0.0034
SF ₁	1.9559	2.455	0.0043	0.0069
SF ₂	1.8600	3.014	0.0137	0.0169
SF ₃	4.6	3.433	0.0190	0.0503
SF ₄	1.752	1	0.0499	0.1749
SF ₅	3.95	1.819	0.0403	0.1749
SF ₆	3.231	1.430	0.0704	0.3181
SF ₇	9.856	2.243	0.0518	0.4549
SF ₈	14.502	1.470	0.0517	1.0204
Focusing lens	$f_T = 0.75$	—	$q_T = 1$	$p_T = 1.5$

(ii) inversely proportional to the BAER from the error mirror to the focusing lens.

2.3. Variance weighing factors

Generally, the disturbances on optics can be attributed into two forms: one is ground vibrations and the other is air turbulence or the acoustic vibrations. In the first case, ground vibrations are transmitted to the optics via the optical trusses, which are mainly made of steel. In the second case, acoustic vibrations directly act on the optics via air. Furthermore, ground vibrations and air turbulence arise from several sources, such as traffic, people working, air compressors, air conditioners, motors, people talking, loudspeakers, and so on.

Several vibrating sources and vibration-sensitive optics exist; thus, normal distribution was utilized to evaluate the system error. Based on Equation (10) to Equation (16), the variance generated by the lenses and mirrors is

$$\Delta_L^2 = \sum_{i=0}^n q_i^2 (\Delta_{Li,1}^2 + \Delta_{Li,2}^2) + \Delta_T^2, \tag{17}$$

$$\Delta_M^2 = \sum_{i=0}^n \left(p_i^2 \sum_{j=0}^{u_i} \Delta_{Mi,j}^2 \right) + \sum_{j=0}^{w_T} p_T^2 \Delta_{MT,j}^2, \tag{18}$$

$$\Delta_{Mi,0}^2 = 0, \tag{19}$$

$$\Delta_{MT,0}^2 = 0, \tag{20}$$

where Δ_L^2 is the total variance in the target generated by the lenses in the spatial filters; Δ_M^2 is the total variance in the target generated by the reflecting mirrors; $\Delta_{Li,1}^2$ and $\Delta_{Li,2}^2$ are the variances of the two lenses in SF_i, respectively; Δ_T^2

is the variance of the focusing lens; u_i is the numbers of the reflecting mirrors between SF_{i,1} and SF_i in SF_i; $\Delta_{Mi,j}^2$ is the mean variance of the *j*th of the u_i reflecting mirrors; and $\Delta_{MT,j}^2$ is the variance of the *j*th of the w_T reflecting mirrors between the last spatial filter and the focusing lens.

Based on Equation (17), the variations of the two lenses in SF_i have the same impact on the target variation, with a factor of q_i^2 . Thus, q_i^2 is defined as the spatial filter lens variation weight factor (SFLVWF). Similarly, in Equation (18), p_i^2 is defined as the spatial filter mirror variation weight factor (SFMVWF). The SFLVWFs and SFMVWFs in a laser-driven ICF facility are illustrated in Figure 3.

3. Sensitivity analysis on SG-II facilities

The SG-II facility is currently composed of three sub-facilities, namely, SG-II Origin, SG-II Additional beam, and SG-II Updated. The previous two facilities use two-pass amplification (TPA) technology, whereas the updated facility uses four-pass amplification (FPA) technology. The TPA or FPA systems were considered as two or four spatial filters, respectively, to analyze the facilities based on the theory in the previous section. In addition, the optical system parameters of the three SG-II facilities are listed in Tables 1–3.

3.1. SFLVWFs in SG-II facilities

The SFLVWFs of the three facilities are shown in Figure 4. Comparing the SFLVWFs in the three facilities, the following conclusions were obtained.

- (i) The most vibration-sensitive spatial filters in SG-II Origin and SG-II Additional beam were SF₆ and SF₇, respectively.
- (i) The SFLVWFs of SF₅ to SF₈ in SG-II Updated were the most vibration-sensitive spatial filters. In fact, the SF₅ to SF₈ were exactly the FPA system, which can also be observed from Table 3.
- (iii) The SFLVWFs of SG-II Origin were much lower than those of SG-II Additional beam and SG-II Updated. This result was mainly due to the fact that the focal length of the focusing lens in SG-II Origin (0.75 m) was shorter than those of the other two facilities (1.575 m for SG-II Additional beam and 2.234 m for SG-II Updated).

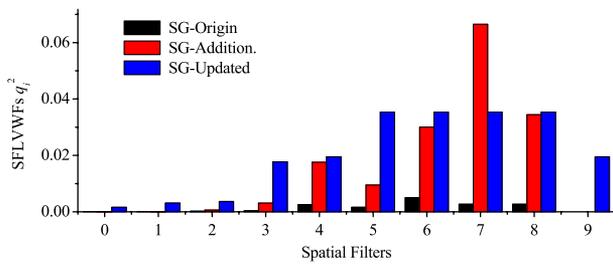


Figure 4. SFLVWFs comparison of the SG-II facilities.

Table 2. Optical parameters of SG-II Additional beam.

Spatial filters	$f_{i,2}$ (m)	m_i	q_i	p_i
SF ₀	1.0	2.000	0.0061	0.0061
SF ₁	1.9559	2.455	0.0076	0.0121
SF ₂	1.8600	3.014	0.0241	0.0297
SF ₃	2.3825	2.960	0.0556	0.0896
SF ₄	1.9971	2.000	0.1327	0.2651
SF ₅	4.0808	1.500	0.0974	0.5302
SF ₆	4.8643	2.120	0.1733	0.7953
SF ₇	5.6547	1.730	0.2579	1.6859
SF ₈	8.4876	1.080	0.1856	2.9167
Focusing lens	$f_T = 1.575$	—	$q_T = 1$	$p_T = 3.1500$

Table 3. Optical parameters of SG-II Updated.

Spatial filters	$f_{i,2}$ (m)	m_i	q_i	p_i
SF ₀	1.800	1	0.0400	0.1441
SF ₁	2.080	1.6	0.0554	0.1441
SF ₂	2.850	1.5	0.0607	0.2306
SF ₃	2.600	2	0.1330	0.3459
SF ₄	16.000	6.4584	0.1396	0.6918
SF ₅	11.117	0.9355	0.1880	4.4680
SF ₆	11.883	1.0689	0.1880	4.1800
SF ₇	11.117	0.9355	0.1880	4.4680
SF ₈	11.883	1.0689	0.1880	4.1800
SF ₉	16.000	1	0.1396	4.4680
Focusing lens	$f_T = 2.234$	—	$q_T = 1$	$p_T = 4.468$

(iv) The SFLVWFs in SG-II Additional beam and SG-II Updated were nearly of the same level. This result is the combined effects of the BAERs and the focal lengths of the lenses. Tables 2 and 3 show that the total BAER of the SG-II Updated (31 times) was much lower than that of SG-II Additional beam (520 times); however, the focal lengths of the lenses in SG-II Updated were much longer than those in SG-II Additional beam, which decreased the SFLVWFs in SG-II Updated to some extent.

3.2. SFMVWFs in SG-II facilities

The SFMVWFs in the three facilities are shown in Figure 5, from which the following conclusions were obtained.

(i) The SFMVWFs grew gradually with decreasing distance to the target in SG-II Origin and SG-II Additional

beam because the beam apertures were magnified step by step in the two facilities.

- (ii) The SFMVWFs from SF₅ to SF₈ in SG-II Updated have the same level, and were much larger than the SFMVWFs in the previous spatial filters in the facility. This phenomenon was caused by the BAER distribution (the beam was magnified 6.46 times in SF₄). These four spatial filters were actually the FPA system, as mentioned previously.
- (iii) The SFMVWFs in SG-II Updated were much larger than those in SG-II Origin and SG-II Additional beam because of the long focal length of its focusing lens ($f_T = 2.234$ m) and the BAER distribution.

3.3. SFLVWFs and SFMVWFs in the FPA system

Compared with the other two facilities, SG-II Updated with the FPA system leveled the SFLVWFs in the FPA system and increased the numbers of sensitive mirrors. The parameters of the FPA system were changed for comparison with the real parameters to find out the features of the FPA system in terms of vibration sensitivities. The parameters are listed in Table 4, and the results are shown in Figures 6–8. The results indicated the following.

- (i) The SFLVWFs in FPA system were the same.
- (ii) The SFLVWFs changed with the BAER and focal lengths of the lenses.
- (iii) The SFMVWFs only changed with the BAER; they were independent of the focal lengths of the lenses.

4. Beam stabilization

4.1. Decrease the vibration sensitivities

As was discussed in the previous two sections in detail, the sensitivities of the optics in laser-driven ICF facilities vary according to the optical parameters. Thus, the appropriate optical parameters that would efficiently enhance the stability of the system should be chosen. Based on Equations (9) and (16), it would be better if:

- (i) the focal lengths of the focusing lens was shorter,
- (ii) the focal lengths of the spatial filters' lenses were longer, and
- (iii) the total BAER was larger.

4.2. Optimization of mechanical structures

Another method to enhance the beam positioning stability is to eliminate the vibration sources, which can be done in two ways: decreasing the mechanical vibration responses and preventing error accumulation. In SG-II facilities, the following methods were utilized.

- (i) Some modules were isolated from other modules, as shown in Figure 8.

Table 4. Experimental parameters in a four-pass amplification system.

Lenses in four-pass amplification (FPA)	CSF-L1 (m)	CSF-L2 (m)	Beam aperture magnification ratio
Real parameters in SG-II updated	11.883	11.117	0.9355
First fictional parameters	20	10	0.5
Second fictional parameters	10	5	0.5

Notes: The SFMVWFs of the reflecting mirrors after spatial filters (p_i^2) in SG-II Origin and SG-II Additional beam were regarded as SF₉ for simplifying the chart. The diagram of FPA system please see Ref. [9].

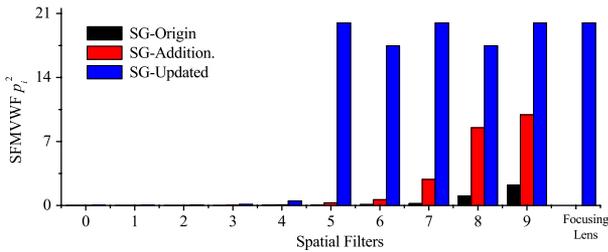


Figure 5. SFMVWF comparison of SG-II facilities.

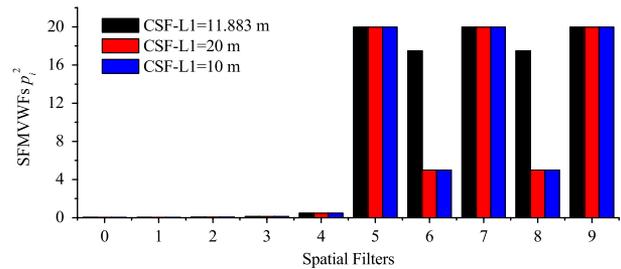


Figure 7. SFMVWF comparison in different FPA systems.

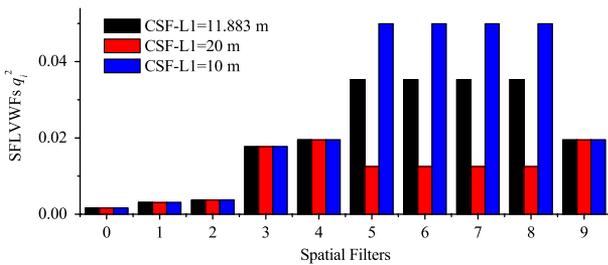


Figure 6. SFLVWF comparison in different FPA systems.



Figure 8. Modules isolated from the other modules.

- (ii) Sensitive optical trusses were filled with concrete. Figure 9 shows that the damping coefficients were increased and the response around the modal frequencies decreased. During the measurements, there were two heavy reflecting supports on the concrete-filled truss, whereas there were none on the blank steel trusses; thus, the compliance curve was even higher in low frequencies and the modal frequencies decreased.
- (iii) The target was relatively fixed with the target focusing lens. Equation (8) and Tables 1–3 show that the error on the focusing lens had much higher contribution to the total beam posing stability. Hence, the target position should be precisely placed at the focus.
- (iv) The beams were bound to prevent error accumulation. Figure 10 shows that four beams were bound, and supported by one support; thus, the four-beam-type errors were decreased to single-beam-type error.

5. Conclusions

This study aimed at stabilizing the beams in laser-driven ICF facilities. The errors on each of optics make different contributions to the targeting stability, and thus, an efficient

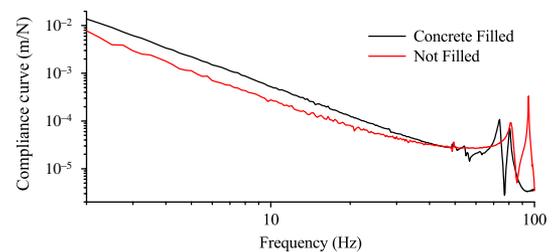


Figure 9. Steel trusses filled with concrete that decreased the responses around modal frequencies.

solution for stabilizing the beams has to eliminate the errors on error-sensitive optics. Therefore, the vibration sensitivities of each optic were initially obtained. The vibration-sensitive optics should be given more attention to enhance the dynamic beam stabilities from the mechanical point of view. The comparison among the three ICF facilities of SG-II indicated that the SG-II Updated facility was the most vibration-sensitive facility because the FPA technology increased the SFMVWFs in the FPA system.



Figure 10. Beams bounded together preventing error accumulation.

This study also pointed out that decreasing the focal length of the focusing lens, increasing the focal lengths of the lenses in the spatial filters, and enlarging the total BAER would decrease the vibration sensitivities of the optics. Moreover, a practical mechanical system design to decrease the beam errors including isolating the vibrating parts and enhancing the precision of target positioning and bound beams to prevent error accumulation must be employed to decrease the impact of vibrations on the optical system.

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