

Dynamic stabilization of plasma instability

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Abstract

The paper presents a review of dynamic stabilization mechanisms for plasma instabilities. One of the dynamic stabilization mechanisms for plasma instability was proposed in the paper [Kawata, *Phys. Plasmas* **19**, 024503 (2012)], based on a perturbation phase control. In general, instabilities emerge from the perturbations. Normally the perturbation phase is unknown, and so the instability growth rate is discussed. However, if the perturbation phase is known, the instability growth can be controlled by a superimposition of perturbations imposed actively. Based on this mechanism we present the application results of the dynamic stabilization mechanism to the Rayleigh–Taylor instability (RTI) and to the filamentation instability as typical examples in this paper. On the other hand, in the paper [Boris, *Comments Plasma Phys. Control. Fusion* **3**, 1 (1977)] another mechanism was proposed to stabilize RTI, and was realized by the pulse train or the laser intensity modulation in laser inertial fusion [Betti *et al.*, *Phys. Rev. Lett.* **71**, 3131 (1993)]. In this latter mechanism, an oscillating strong force is applied to modify the basic equation, and consequently the new stabilization window is created. Originally the latter was proposed by Kapitza. We review the two stabilization mechanisms, and present the application results of the former dynamic stabilization mechanism.

Keywords: dynamic instability stabilization; filamentation instability; plasma instability; Rayleigh–Taylor instability; stabilization of instability

1. Introduction

Dynamic stabilization mechanisms for plasma instabilities are reviewed and discussed in this paper. So far, the dynamic stabilization for the Rayleigh–Taylor instability (RTI)^[1–6] has been proposed and discussed intensively in order to obtain a uniform compression^[7, 8] of a fusion fuel pellet in inertial confinement fusion. The RTI dynamic stabilization was found many years ago^[1, 2] and is important in inertial fusion. It was implemented that the oscillation amplitude of the driving acceleration should be sufficiently large to stabilize RTI^[1–6]. In inertial fusion, the fusion fuel compression is essentially important to reduce an input driver energy^[7, 8], and the implosion uniformity is one of critical issues to compress the fusion fuel pellet stably^[9, 10]. Therefore, the RTI stabilization or mitigation is attractive to minimize the fusion fuel mix.

On the other hand, instability grows from a perturbation in general, and normally the perturbation phase is unknown. Therefore, it would be difficult to control the perturbation

phase, and usually the instability growth rate is discussed. However, if the perturbation phase is controlled and known, we can find a new way to control the instability growth. One of the most typical and well-known mechanisms is the feedback control in which the perturbation phase is detected and the perturbation growth is controlled or mitigated or stabilized. In plasmas it is difficult to detect the perturbation phase and amplitude. However, even in plasmas, if we can actively impose the perturbation phase by the driving energy source wobbling or so, and therefore, if we know the phases of the perturbations, the perturbation growth can be controlled in a similar way as shown in Figure 1^[11, 12]. In instabilities, one mode of an initial perturbation, from which an instability grows, may have the form of $a = a_0 e^{ikx + \gamma t}$, where a_0 is the amplitude, $k = 2\pi/\lambda$ is the wave number, λ the wave length and γ the growth rate of the instability. An initial perturbation example is shown in Figure 1(a). At $t = 0$ the perturbation is imposed. The initial perturbation may grow at instability onset. After Δt , if the feedback control works on the system, another perturbation, which has an inverse phase with the detected amplitude at $t = 0$, is actively imposed (see Figure 1(b)), and then the actual perturbation amplitude is very well mitigated as

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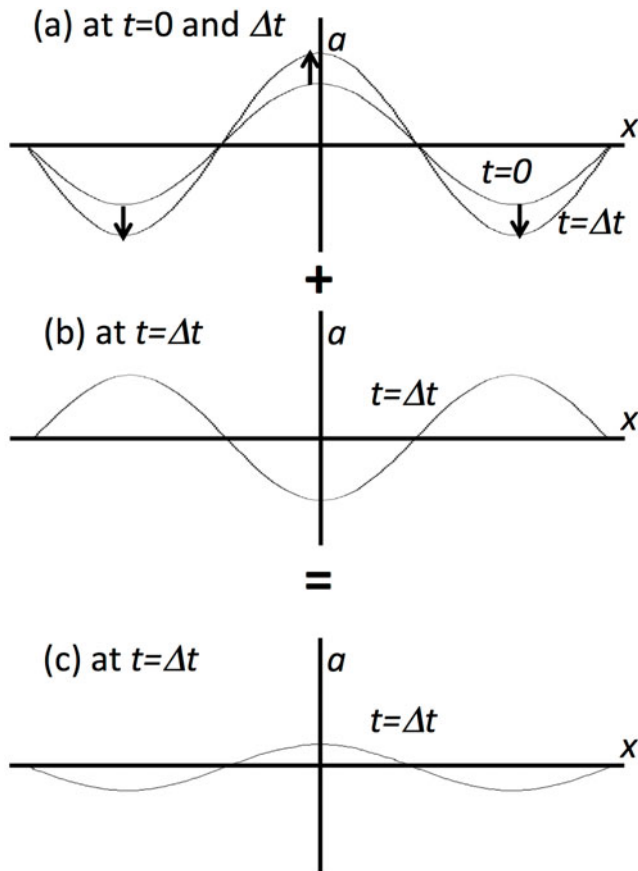


Figure 1. An example concept of feedback control. (a) At $t = 0$ a perturbation is imposed. The initial perturbation may grow at instability onset. (b) After Δt , if the feedback control works on the system, another perturbation, which has an inverse phase with the detected amplitude at $t = 0$, is actively imposed, so that (c) the actual perturbation amplitude is mitigated very well after the superposition of the initial and additional perturbations.

shown in Figure 1(c). This is an ideal example for the instability mitigation. This control mechanism is apparently different from the dynamic stabilization mechanism shown in the previous works in Refs. [1–6]. For example, the growth of the filamentation instability^[13–17] driven by a particle beam or jet could be controlled by the beam axis oscillation or wobbling. The oscillating and modulated beam induces the initial perturbation and also could define the perturbation phase. Therefore, the successive phase-defined perturbations are superimposed, and we can use this property to mitigate the instability growth. Another example can be found in heavy ion beam inertial fusion; the heavy ion accelerator could have a capability to provide a beam axis wobbling with a high frequency^[18–20]. The wobbling heavy ion beams also define the perturbation phase. This means that the perturbation phase is known, and so the successively imposed perturbations are superimposed on plasmas. We can again use the capability to reduce the instability growth by the phase-controlled superposition of perturbations. In this paper we discuss and clarify the

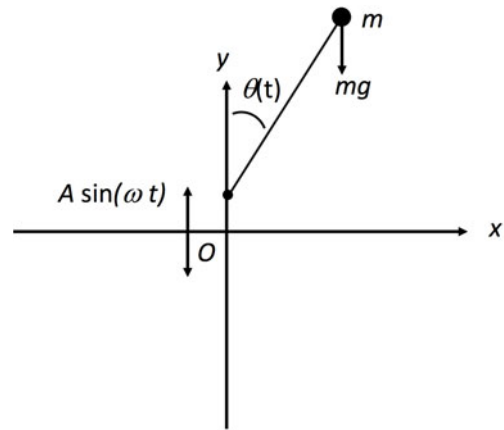


Figure 2. Kapitza's pendulum, which can be stabilized by applying an additional strong and rapid acceleration $A \sin \omega t$.

dynamic mitigation mechanisms for plasma instabilities. First, we discuss the dynamic stabilization mechanism based on Refs. [1–6, 21] to stabilize the RTI by applying the strong and rapid acceleration oscillation. Then we present the other dynamic stabilization mechanism proposed in Refs. [12, 20, 22, 23], which is applied to the RTI and filamentation instability stabilization.

2. Dynamic stabilization of plasma instability under strong driving force oscillation

In Refs. [1–3], one dynamic stabilization mechanism was proposed to stabilize the RTI based on the strong oscillation of acceleration, which was realized, for example, by the picket fence pulse train or the laser intensity modulation in laser inertial fusion^[4]. In this mechanism, the total acceleration oscillates strongly, and so the additional oscillating force is added to create a new stable window in the system. Originally this dynamic stabilization mechanism was proposed by Kapitza^[21], and it was applied to the stabilization of an inverted pendulum. The inverted pendulum is an unstable system, a strongly and rapidly oscillating acceleration is applied on the system in Ref. [21], and then the inverted pendulum system has a stable window. In this case, the equation for the unstable system is modified, and has another force term coming from the oscillating acceleration. In this mechanism, the growth rate is modified by the strongly oscillating acceleration.

When the inverted pendulum shown in Figure 2 is subjected by a strongly oscillating acceleration $A \sin \omega t$, we obtain the following Mathieu-type equation^[24] for $\theta(t)$:

$$\frac{d^2\theta(t)}{dt^2} = \frac{g}{l}\theta(t) - A\omega^2\theta(t)\sin\omega t. \quad (1)$$

Here l is the length of the pendulum. When $A = 0$, the inverted pendulum becomes unstable. However, the second

term of the right-hand side is added to the system, and stable windows appear in the inverted pendulum system^[21, 24]. In Equation (1), the stability condition is described as $A - 0.5 < 2g/(l\omega^2) < A^2$ ^[24]. The stability condition shows that the additional acceleration oscillation at the second term of the right-hand side of Equation (1) should be very fast, and the amplitude of A must satisfy the stability condition.

This dynamic stabilization mechanism works on the inverted pendulum in Figure 1. However, it would be difficult to apply this mechanism to our tall buildings, bridges or large structures in our society.

In laser inertial fusion, this dynamic stabilization mechanism was proposed and applied to stabilize the RTI based on the strong oscillation of acceleration^[3, 4], which was realized by the picket fence pulse train or the laser intensity modulation in laser inertial fusion^[4]. In this mechanism, the total acceleration strongly oscillates, and so the additional oscillating force is added to create a new stable window in the fuel pellet implosion in laser inertial fusion. In inertial fusion, the spherical fuel pellet should be compressed to a high density, for example, a thousand times of the solid density^[8–10]. The fusion fuel is imploded spherically by a large inward acceleration. The typical implosion acceleration is about 10^{13} m/s², and lasts for 1–10 ns. During the implosion time, the driver input energy, introduced by the laser-pulse train series, would induce the strong implosion acceleration oscillation, which contributes to stabilizing the RTI during the fuel pellet implosion^[3, 4, 25, 26].

In Ref. [27], this dynamic stabilization mechanism is applied to the two-stream instability stabilization, in which the classical two-stream instability driven by a constant relative drift velocity is modified by the additional oscillation on the relative velocity. The time-dependent drift velocity opens a new stable window in the two-stream instability.

3. Dynamic stabilization of plasma instability under a phase control

In plasmas the perturbation phase and amplitude cannot be measured dynamically. However, by using a wobbling beam or an oscillating beam or a rotating beam or so^[18, 19], the initial perturbation is actively imposed, and so the initial perturbation phase and amplitude are defined actively. In this case, the amplitude and phase of the unstable perturbation cannot be detected, but can be defined by the input driver beam wobbling at least in the linear phase. In plasmas it would be difficult to realize a perfect feedback control, but a part of it can be adapted to the instability mitigation in plasmas. Actually, heavy ion beam accelerators would provide a controlled wobbling or oscillating beam with a high frequency^[18–20, 28]. An intense electron beam axis can be wobbled in its controlled way, and thus provides defined phase and amplitude of perturbations.

If the energy driver beam wobbles uniformly in time, the imposed perturbation for a physical quantity of F at $t = \tau$ may be written as

$$F = \delta F e^{i\Omega\tau} e^{\gamma(t-\tau) + i\vec{k}\cdot\vec{x}}. \quad (2)$$

Here δF is the amplitude, Ω the wobbling or oscillation frequency, and $\Omega\tau$ the phase shift of superimposed perturbations. At each time $t = \tau$, the wobbler provides a new perturbation with the controlled phase shifted and amplitude defined by the driving wobbler itself. After the superposition of the perturbations, the overall perturbation is described as

$$\int_0^t d\tau \delta F e^{i\Omega\tau} e^{\gamma(t-\tau) + i\vec{k}\cdot\vec{x}} \propto \frac{\gamma + i\Omega}{\gamma^2 + \Omega^2} \delta F e^{\gamma t} e^{i\vec{k}\cdot\vec{x}}. \quad (3)$$

At each time of $t = \tau$ the driving wobbler provides a new perturbation with the shifted phase. Then each perturbation grows with the factor of $e^{\gamma t}$. At $t > \tau$ the superimposed overall perturbation growth is modified as shown above. When $\Omega \gg \gamma$, the perturbation amplitude is reduced by the factor of γ/Ω , compared with the pure instability growth ($\Omega = 0$) based on the energy deposition nonuniformity^[12, 22, 23, 29].

Figure 3 shows the superimposed perturbations decomposed, and at each time the phase-defined perturbation is imposed actively by the driving wobbler. The perturbations are superimposed at the time t . The wobbling trajectory is under control, for example, by a beam accelerator or so, the superimposed perturbation phase and amplitude are controlled, and the overall perturbation growth is also controlled.

From the analytical expression for the physical quantity F in Equation (3), the mechanism proposed in this paper does not work, when $\Omega \ll \gamma$. Only modes, fulfilling the condition of $\Omega \geq \gamma$, can experience the instability mitigation through a wobbling process. For RTI, the growth rate γ tends to become larger for a short wavelength. If $\Omega \ll \gamma$, the modes cannot be mitigated. In addition, if there are other sources of perturbations in the physical system and if the perturbation phase and amplitude are not controlled, this dynamic mitigation mechanism also does not work. For example, if the sphericity of an inertial fusion fuel target is degraded, the dynamic mitigation mechanism does not work. In this sense the dynamic mitigation mechanism is not almighty. Especially for a uniform compression of an inertial fusion fuel all the instability stabilization and mitigation mechanisms would contribute to releasing the fusion energy.

Figure 4 shows an example simulation for RTI, which has one mode. In this example, two stratified fluids are superimposed under an acceleration of $g = g_0 + \delta g$. The density jump ratio between the two fluids is 10/3. In this specific case the wobbling frequency Ω is γ , the amplitude of δg is $0.1g_0$, and the results shown in Figure 4 are those at $t = 5/\gamma$. In Figure 4(a) δg is constant and drives the RTI as usual, and in Figure 4(b) the phase of δg oscillates with the frequency of Ω as stated above for the dynamic instability

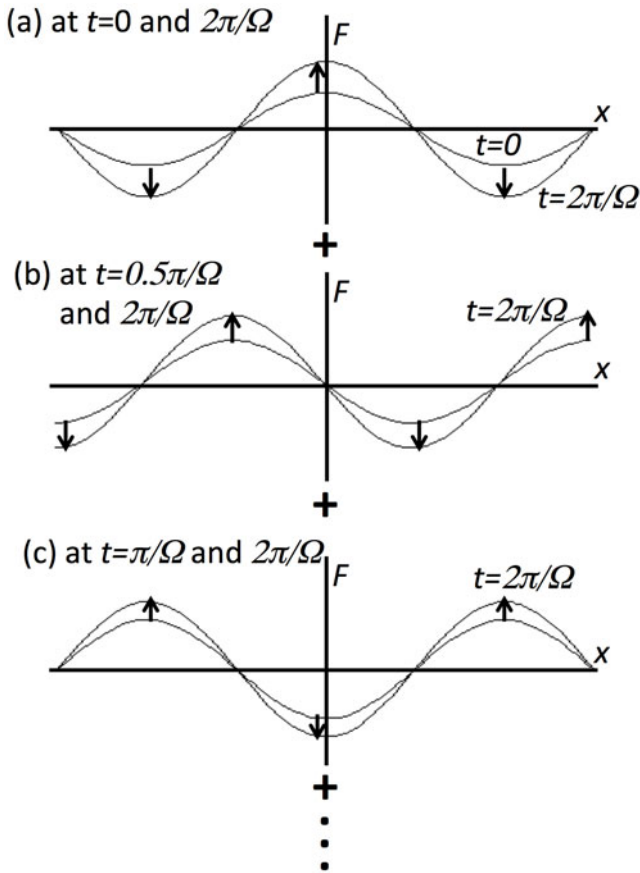


Figure 3. Superposition of perturbations defined by the wobbling driver beam. At each time the wobbler provides a perturbation, whose amplitude and phase are defined by the wobbler itself. If the system is unstable, each perturbation is a source of instability. At a certain time the overall perturbation is the superposition of the growing perturbations. The superimposed perturbation growth is mitigated by the beam wobbling motion.

stabilization in this section. The RTI growth mitigation ratio is 72.9% in Figure 4. The growth mitigation ratio is defined by $(H_0 - H_{\text{mitigate}})/H_0 \times 100\%$. Here H is defined as shown in Figure 4(a), H_0 shows the deviation amplitude of the two-fluid interface in the case in Figure 4(a) without the oscillation ($\Omega = 0$), and H_{mitigate} presents the deviation for the other cases with the oscillation ($\Omega \neq 0$). The example simulation results support well the effect of the dynamic mitigation mechanism. Other multi-modes RTI analyses are found in Ref. [11].

In order to check the robustness of the dynamic instability mitigation mechanism^[29], here we study the effects of the change in the phase, the amplitude and the wavelength of the wobbling perturbation δF , that is, δg in Figure 4 on the dynamic instability mitigation.

When the perturbation amplitude $\delta F = \delta F(t)$ depends on time or oscillates slightly in time, the dynamic mitigation mechanism is examined first. We consider $\delta F(t) = \delta F_0(1 + \Delta e^{i\Omega't})$ in Equation (1). Here $\Delta \ll 1$.

In this case, Equation (3) is modified as follows:

$$\int_0^t d\tau \delta F e^{i\Omega\tau} e^{\gamma(t-\tau)+i\vec{k}\cdot\vec{x}} \propto \left\{ \frac{\gamma + i\Omega}{\gamma^2 + \Omega^2} + \Delta \frac{\gamma + i(\Omega + \Omega')}{\gamma^2 + (\Omega + \Omega')^2} \right\} \delta F_0 e^{\gamma t} e^{i\vec{k}\cdot\vec{x}}. \quad (4)$$

When $\Delta \ll 1$ in Equation (4), just a minor effect appears on the dynamic mitigation of the instability.

We also performed the fluid simulations. In the simulations $\delta g(t) = \delta g(1 - \Delta \sin \Omega't)$. The RTI is simulated again based on the same parameter values shown in Figure 4 except the perturbation amplitude oscillation $\delta F(t)$. In the simulations we employ $\Omega' = 3\Omega$, Ω and $\Omega/3$ in Equation (4). For $\Delta = 0.1$ and 0.3 , and for $\Omega' = 3\Omega$, Ω and $\Omega/3$, the RTI growth reduction ratio is 54.9%–73.2% at $t = 5/\gamma$. Figure 5 shows the results for $\Delta = 0.3$. The results by the fluid simulations and Equation (4) demonstrate that the perturbation amplitude oscillation $\delta F = \delta F(t)$ is uninfluential as long as $\Delta \ll 1$.

When the oscillation frequency Ω of the perturbation δF depends on time ($\Omega = \Omega(t)$), the time-dependent frequency means that $\Omega(t)$ would consist of multiple frequencies: $e^{i\Omega t} = \sum_i \Delta_i e^{i\Omega_i t}$. In this case Equation (3) becomes

$$\int_0^t d\tau \delta F e^{i\Omega\tau} e^{\gamma(t-\tau)+i\vec{k}\cdot\vec{x}} \propto \sum_i \Delta_i \frac{\gamma + i\Omega_i}{\gamma^2 + \Omega_i^2} \delta F e^{\gamma t} e^{i\vec{k}\cdot\vec{x}}. \quad (5)$$

The result in Equation (5) shows that the highest frequency of Ω_i contributes to the instability mitigation. In a real system the highest frequency would be the original wobbling frequency Ω or so, and the largest amplitude of Δ_i is also that for the original wobbling mode. So when the frequency change is slow, the original wobbler frequency of Ω contributes to the mitigation.

The fluid simulations are also done for the RTI with $\Omega(t) = \Omega(1 + \Delta \sin \Omega't)$ together with the same parameter values employed in Figure 4. In this case $\Delta = 0.1$ and 0.3 , and $\Omega' = 3\Omega$, Ω and $\Omega/3$. The growth reduction ratio was 66.9%–74.0% at $t = 5/\gamma$. Figure 6 presents the simulation results for $\Delta = 0.3$. The little oscillation of the imposed perturbation oscillation frequency $\Omega(t)$ has a minor effect on the dynamic instability mitigation.

When the wobbling wavelength $\lambda = 2\pi/k$ depends on time, one can expect as follows in a real system: $k(t) = k_0 + \Delta k e^{i\Omega_k t}$ and $k_0 \gg \Delta k$. In this case the wobbling wavelength changes slightly in time, and Equation (3) becomes as follows:

$$\int_0^t d\tau \delta F e^{i\Omega\tau} e^{\gamma(t-\tau)+ik\cdot x} \propto \delta F e^{\gamma t + ik_0 \cdot x} \int_0^t d\tau e^{(i\Omega - \gamma)\tau} \sum_{m=-\infty}^{\infty} i^m J_m(\Delta k \cdot x) e^{im\Omega_k \tau}$$

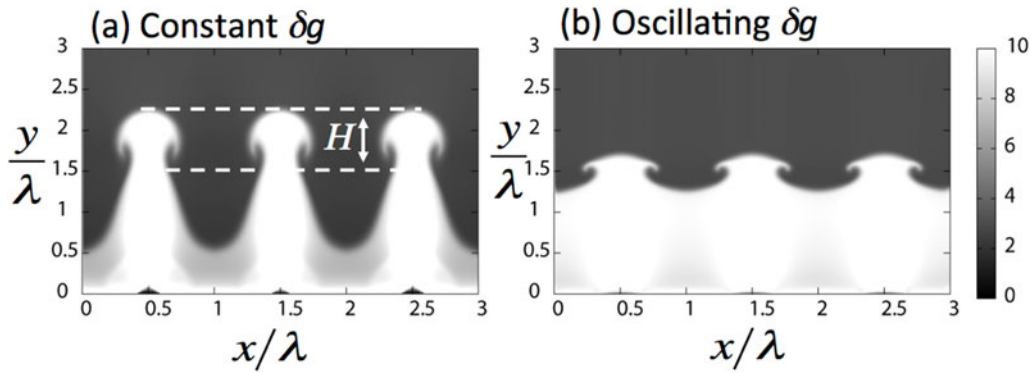


Figure 4. Example simulation results for the Rayleigh–Taylor instability (RTI) mitigation. δg is 10% of the acceleration g_0 and oscillates with the frequency of $\Omega = \gamma$. As shown above and in Equation (3), the dynamic instability mitigation mechanism works well to mitigate the instability growth.

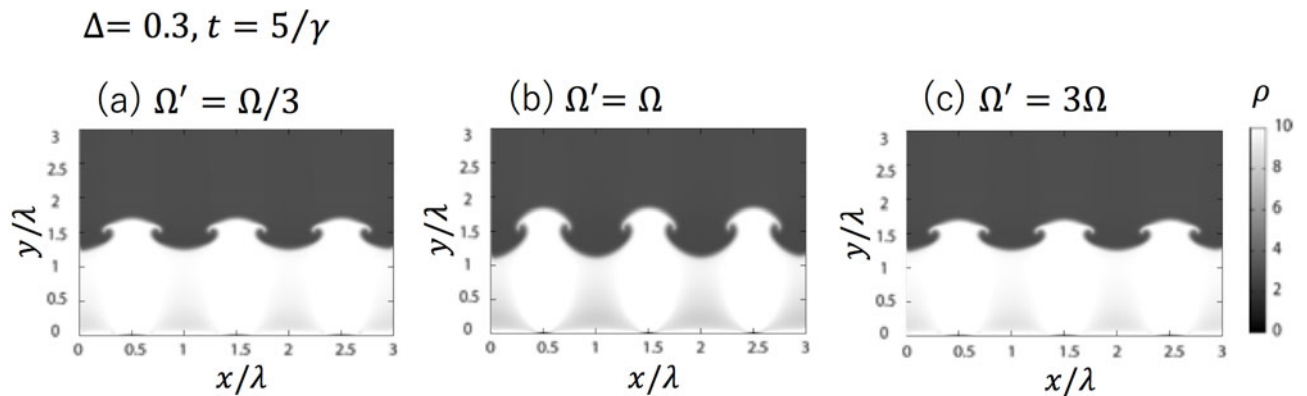


Figure 5. Fluid simulation results for the RTI mitigation for the time-dependent $\delta g(t) = \delta g - \Delta \sin \Omega' t$ at $t = 5/\gamma$. In the simulations $\Delta = 0.3$, and (a) $\Omega' = \Omega/3$, (b) $\Omega' = \Omega$ and (c) $\Omega' = 3\Omega$. The dynamic mitigation mechanism is robust against the time change of the perturbation amplitude $\delta g(t)$.

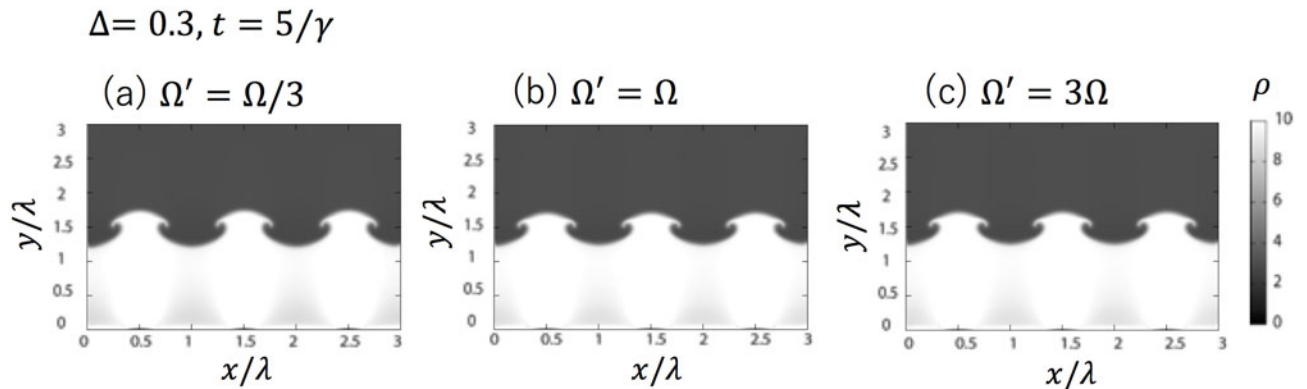


Figure 6. Fluid simulation results for the RTI mitigation for the time-dependent wobbling frequency $\Omega(t) = \Omega(1 + \Delta \sin \Omega' t)$ at $t = 5/\gamma$. In the simulations $\Delta = 0.3$, and (a) $\Omega' = \Omega/3$, (b) $\Omega' = \Omega$ and (c) $\Omega' = 3\Omega$. The dynamic mitigation mechanism is also robust against the time change of the perturbation frequency $\Omega(t)$.

$$\begin{aligned} &\propto \sum_{m=-\infty}^{\infty} i^m J_m(\Delta k \cdot x) \int_0^t d\tau e^{i(\Omega + m\Omega'_k)\tau - \gamma\tau} \\ &\propto \sum_{m=-\infty}^{\infty} i^m J_m(\Delta k \cdot x) \frac{\gamma + i(\Omega + m\Omega'_k)}{\gamma^2 + (\Omega + m\Omega'_k)^2}. \end{aligned} \quad (6)$$

Here J_m is the Bessel function of the first kind. Equation (6) demonstrates that the instability growth reduction

effect is not degraded by the small change in the wobbling wavelength. In actual situations the mode $m = 0$ contributes mostly to the instability mitigation, and in this case the original reduction effect shown in Equation (3) is recovered.

The fluid simulations are also performed for this case $k(t) = k_0 + \Delta k e^{i\Omega'_k t}$. Figure 7 shows the example simulation results for $\Delta k/k_0 = 0.3$ and $\Omega'_k = 3\Omega$, Ω and $\Omega/3$. Figure 7(a) shows the RTI growth reduction ratio of 61.3%

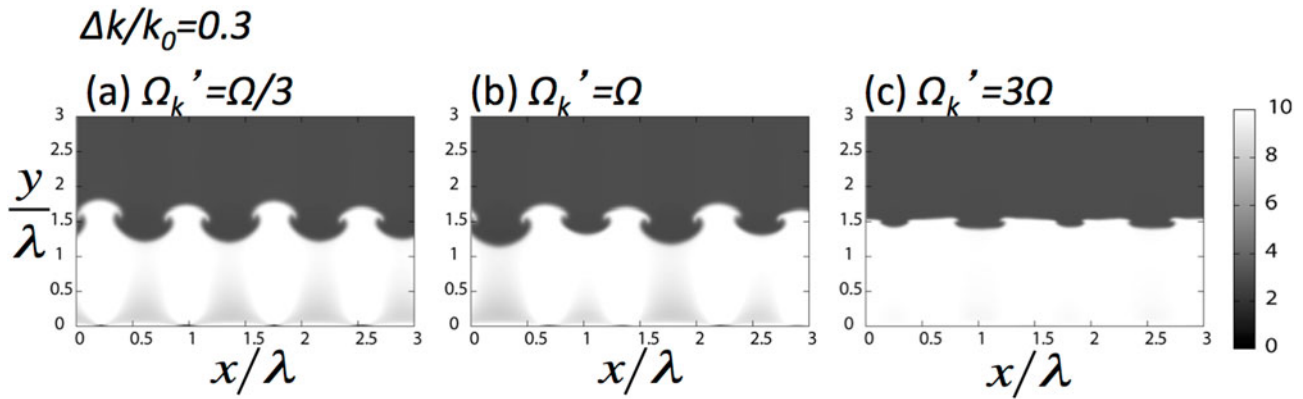


Figure 7. Fluid simulation results for the RTI mitigation for the time-dependent wobbling wavelength $k(t) = k_0 + \Delta k e^{i\Omega'_k t}$, at $t = 5/\gamma$. In the simulations $\Delta k/k_0 = 0.3$, and (a) $\Omega'_k = \Omega/3$, (b) $\Omega'_k = \Omega$ and (c) $\Omega'_k = 3\Omega$. The dynamic mitigation mechanism is also robust against the time change of the perturbation wavelength $k(t)$.

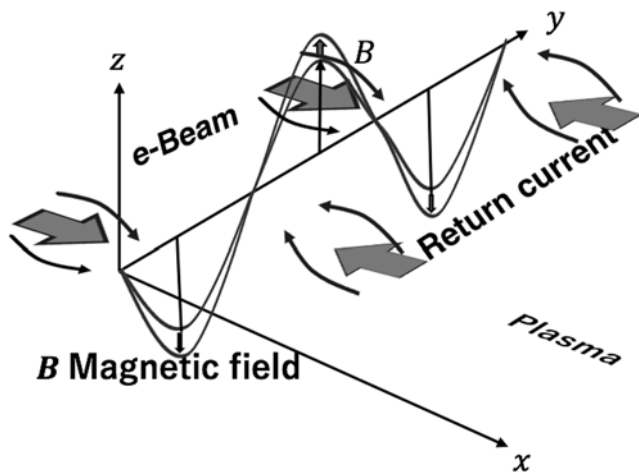


Figure 8. Filamentation instability. In this case an electron beam has a density perturbation in the transverse direction, and is injected into a plasma. In the plasma return current is induced to compensate for the electron beam current. The perturbed electron beam itself defines the filamentation instability phase, and the e-beam axis oscillates in the y direction in this example case. Therefore, the filamentation instability is mitigated by the dynamic stabilization mechanism.

for $\Omega'_k = \Omega/3$, Figure 7(b) shows 68.0% for $\Omega'_k = \Omega$, and Figure 7(c) shows 93.3% for $\Omega'_k = 3\Omega$ at $t = 5/\gamma$. For a realistic situation $\Omega'_k \sim \Omega$, where Ω is the wobbling or modulation frequency.

All the results shown above demonstrate that the dynamic instability mitigation mechanism proposed is rather robust against the changes in the amplitude, the phase and the wavelength of the wobbling or modulating perturbation of δF in general or δg in RTI.

Another possible example is the filamentation instability^[13–16, 23] as shown in Figure 8 schematically. In this example, an electron beam is injected into a plasma, and the electron beam has a density or current modulation in the transverse direction. The modulation is the source of the perturbation defined actively by the electron beam itself, and so the perturbation phase is defined. From the initial

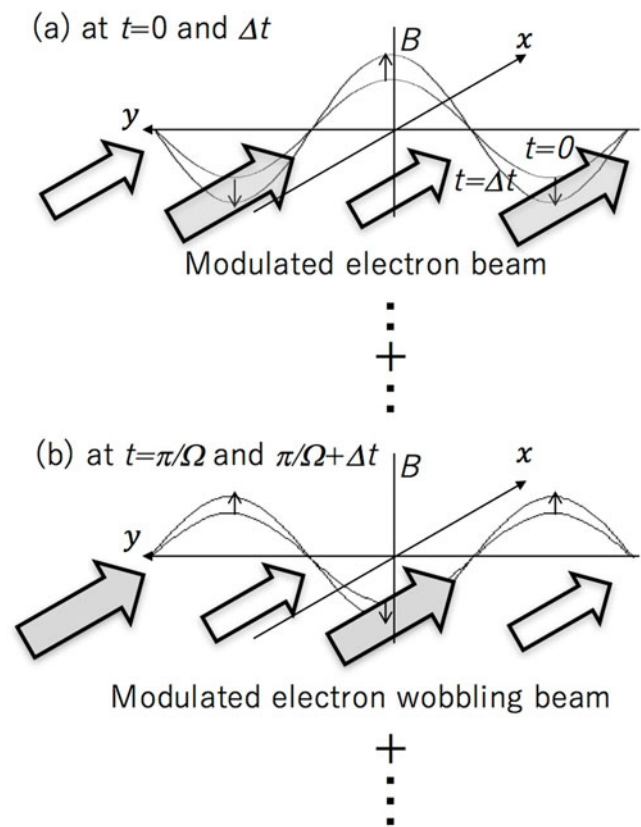


Figure 9. Dynamic stabilization mechanism for the filamentation instability. (a) A modulated electron beam is imposed to induce the filamentation instability. The electron beam axis is wobbled or oscillates transversally with its frequency of Ω . (b) At a later time its phase-shifted perturbation is additionally imposed by the electron beam itself. The overall perturbation is the superposition of all the perturbations, and the filamentation instability is dynamically stabilized.

perturbation the filamentation instability grows with its growth rate. In this filamentation instability a magnetic field perturbation is induced by the electron beam modulation, the electron trajectories are bent and then the electron beam perturbation is further enhanced. Consequently the magnetic

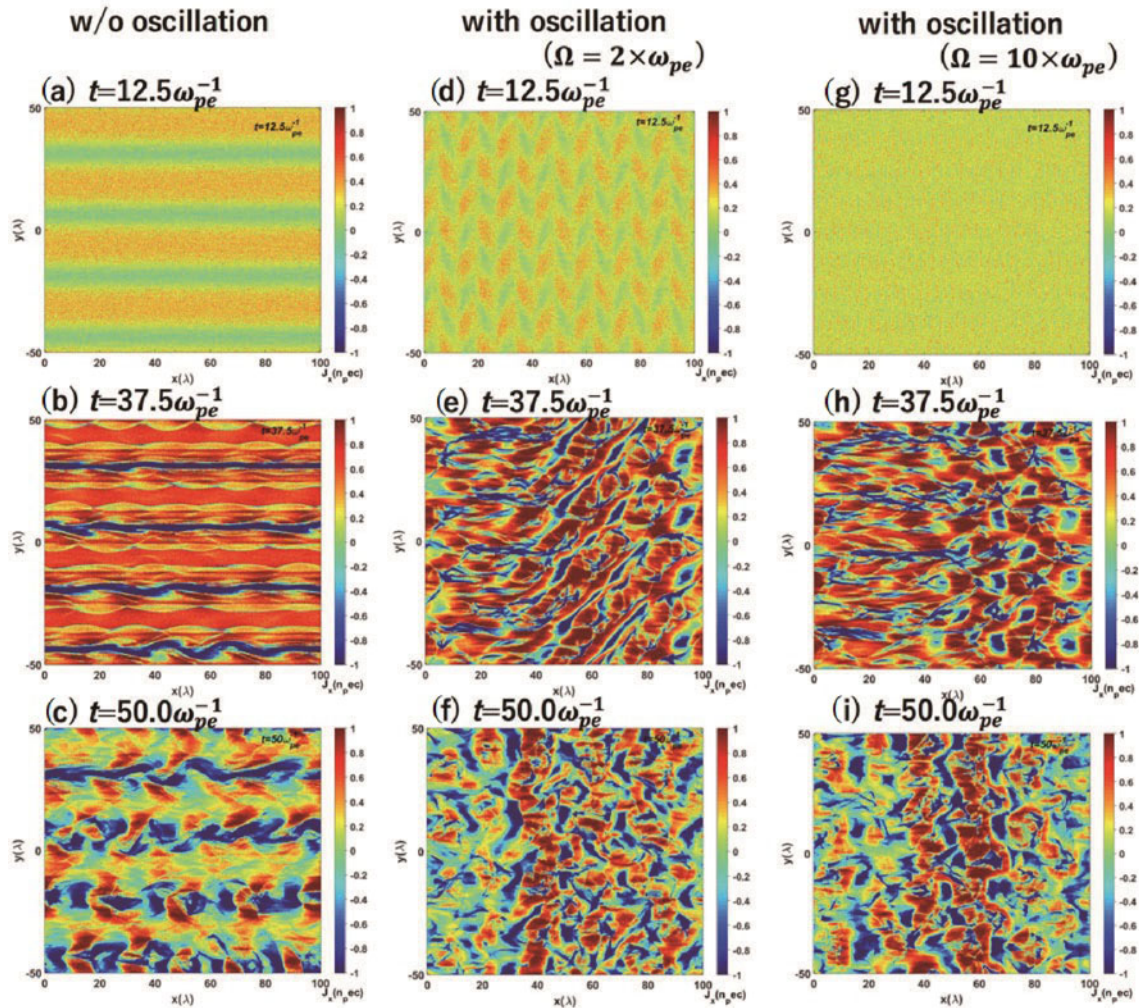


Figure 10. Filamentation instability simulation results without and with the electron beam oscillation. The current density J_x is shown at each time step. When the electron beam axis oscillates in the y direction ((d)–(f) and (g)–(i)), the filamentation instability growth is clearly mitigated.

field is also enhanced. If the electron beam axis oscillates transversally, the perturbations, which could have different phases, are successively imposed in the system and the dynamic mitigation mechanism works.

It is assumed that an electron beam moving in the x direction with v_{be} has a small density perturbation in the transverse direction (y). The perturbed electron beam is injected into a plasma as shown in Figure 9. The current density perturbation induces the filamentation instability^[13–16, 23], in which the perturbation of the transverse magnetic field in the z direction grows, the electron trajectories are bent by the magnetic field, and consequently the current perturbation is enhanced.

The growth rate of the filamentation instability is expressed by $\gamma_F \cong \beta \sqrt{\alpha / \gamma_b} \omega_{pe}$, where $\beta = v_{be}/c$, $\alpha = n_{be}/n_p$, n_{be} is the electron beam number density, n_p the number density of the background plasma electrons, $\gamma_b = 1/\sqrt{1 - \beta^2}$, and ω_{pe} the plasma frequency of the background plasma electrons.

Figure 9 shows the dynamic stabilization mechanism for the filamentation instability schematically. The input electron beam is injected into a plasma, and the electron beam has a current modulation in the y direction. The electron beam current modulation defines actively the filamentation phase as shown in Figure 9(a). After a short time of Δt , the filamentation instability grows. Then the electron beam oscillates in the y direction as shown in Figure 9(b), and the electron beam modulation also moves in the y direction. The new perturbation with the shifted phase is applied, and the perturbations grow. The overall instability growth should be defined by the sum of all the perturbations at t , and the filamentation instability is dynamically stabilized as shown in Figure 1(c).

In order to verify the filamentation instability stabilization, we perform 2-dimensional particle-in-cell (PIC) simulations. As an example case, we use the following parameter values: $\alpha = n_{be}/n_p = 1/9$, $\beta = v_{be}/c = 0.9$, $v_{pe}/c = -0.1$, the temperatures of the beam electrons, the background

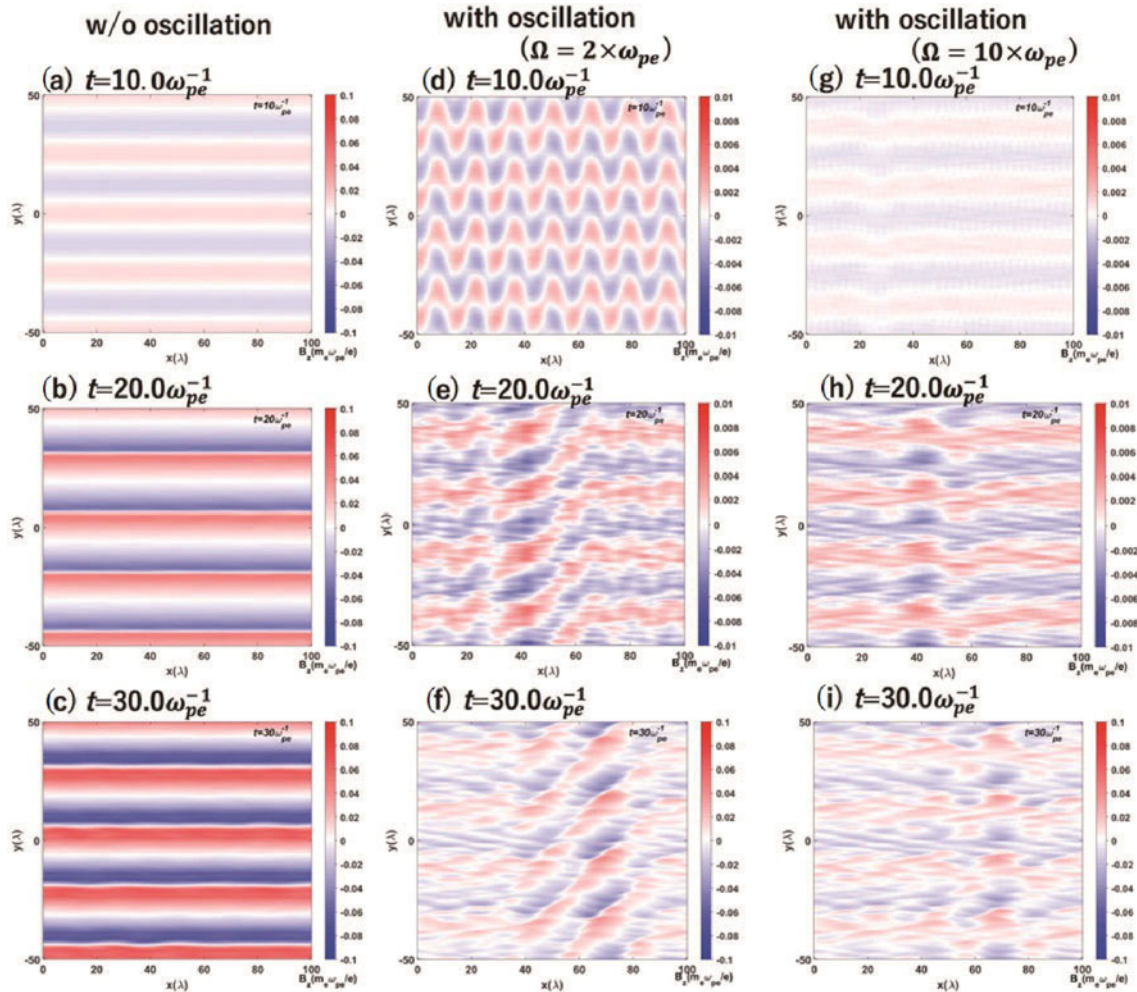


Figure 11. Magnetic field B_z for the filamentation instability without and with the electron beam oscillation.

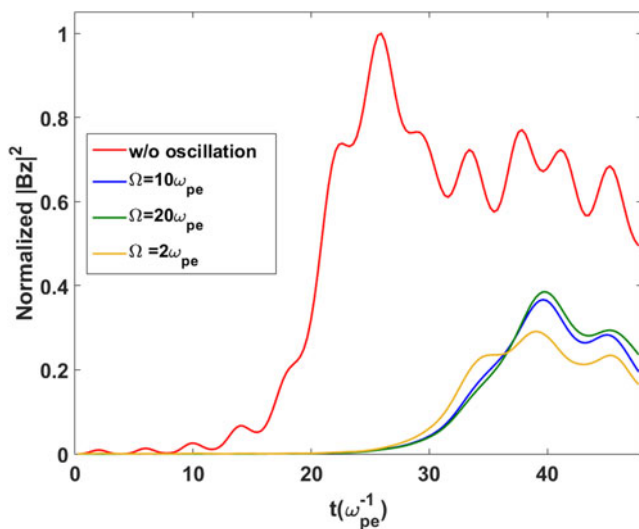


Figure 12. Histories of the normalized magnetic field energy $U_{B_z} \propto |B_z|^2$. When the electron beam transverse oscillation frequency Ω in y becomes larger than or comparable to γ_F , the dynamic stabilization effect is remarkable.

electrons and the background ions are 100 eV. In our simulations, $n_p = 1.00 \times 10^{-3} \times 4\pi^2 \epsilon_0 m_e c^2 / (\lambda e)^2$, the time is normalized by $1/\omega_{pe}$ and the scale length is normalized by λ .

Figures 10–12 show the simulation results for the filamentation instabilities with and without the electron beam oscillation. The electron beam perturbation is imposed in the beam density, and the amplitude is 10%. The oscillation amplitude is 5λ in the y direction in these specific cases. The electron beam oscillation frequency Ω is $2\omega_{pe}$, $10\omega_{pe}$ and $20\omega_{pe}$ ($> \gamma_F$). Figure 10 presents the current density for the cases without and with the electron beam oscillation in the y direction. Figure 11 show the magnetic field B_z distribution. The stabilization effect of the filamentation instability is clearly demonstrated in Figure 11. Figure 12 shows the magnetic field energy history. The dynamic stabilization ratio is introduced by $R_r = [1 - (U_{B_z}/U_{B_z0})] \times 100\%$, where U_{B_z} shows the magnetic field energy. U_{B_z} is normalized by the magnetic field energy U_{B_z0} obtained without the electron beam oscillation. At $t = 35\omega_{pe}^{-1}$, the stabilization ratio $R_r = 58.6\%$ in the case of $\Omega = 2\omega_{pe}$. When the electron beam transverse oscillation frequency Ω in the y direction

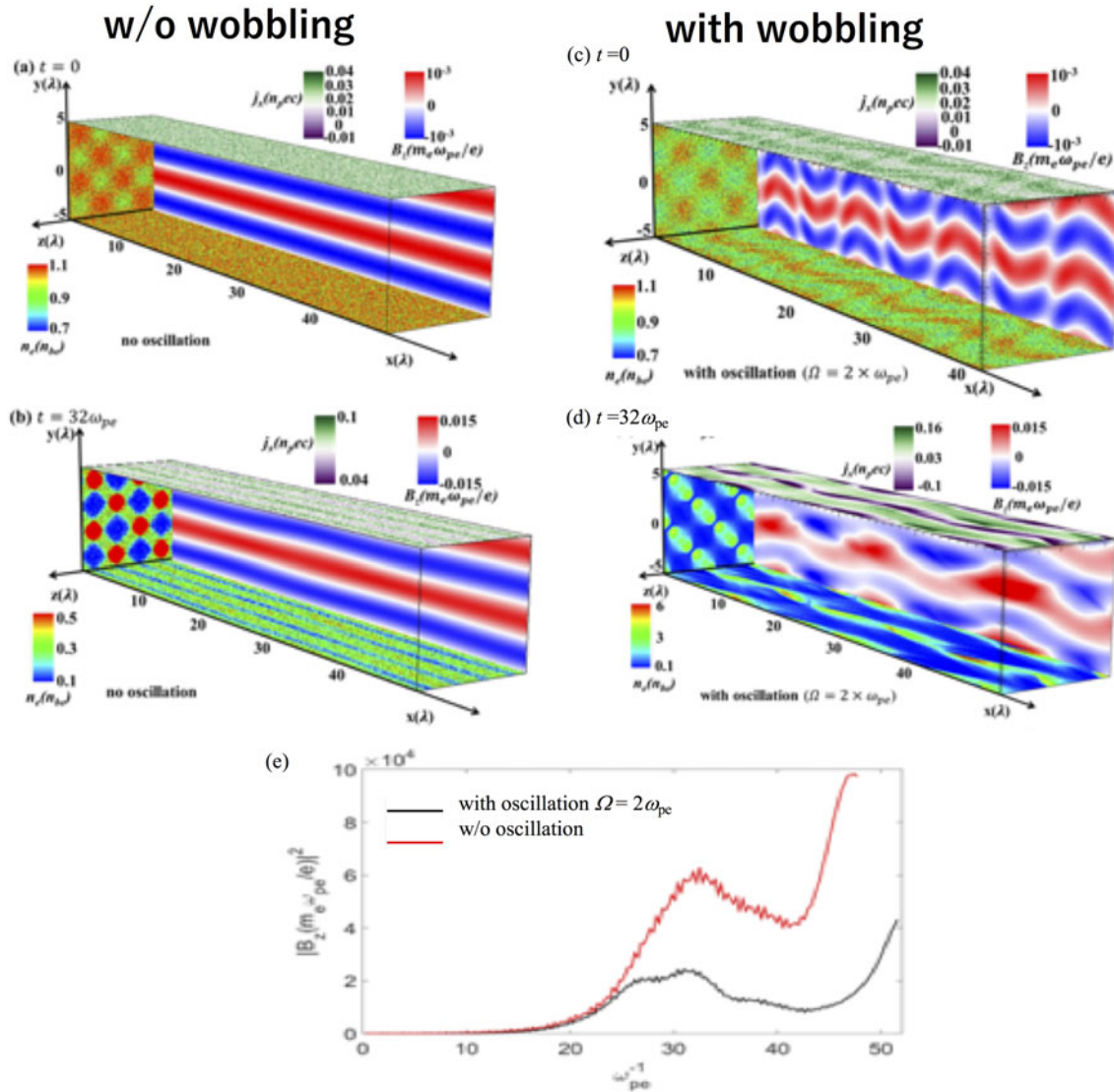


Figure 13. 3D PIC simulation results for the filamentation instability growth at (a) $t = 0$ and (b) $t = 32\omega_{pe}$ without the electron beam wobbling motion, and (c) $t = 0$ and (d) $t = 32\omega_{pe}$ with the wobbling motion. The histories of the normalized magnetic field energy $U_{Bz} \propto |B_z|^2$ is shown in (e). When the electron beam transverse oscillation frequency Ω in y becomes larger than or comparable to γ_F , the dynamic stabilization effect is also remarkable. The 3D simulation results also confirm the instability mitigation mechanism in the plasma.

becomes larger than or comparable to γ_F , the dynamic stabilization effect is remarkable. Figure 13 presents the 3D PIC simulation results for the filamentation instability under the same parameter values as those in Figures 10–12. The results shown in Figures 10–13 demonstrate that the dynamic stabilization mechanism works well to stabilize the filamentation instability.

4. Discussions and summary

In this paper we have discussed the dynamic stabilization in plasmas. The dynamic stabilizations^[1–4], based on the

‘Kapitza’s pendulum’^[21], introduce a new strong oscillating force into the basic equation, and then the governing equation is modified by the additional term to create a new stable window in the system. Therefore, the growth rate is modified, and the stable window appears in the system. The dynamic stabilization mechanism has been applied to the inverted pendulum^[21], to a fuel target implosion in laser inertial fusion^[4], and also to the stabilization of the two-stream instability^[27]. Another dynamic stabilization mechanism, which is also based on the strong forced field but is different from the ‘Kapitza’s pendulum’, was also proposed and applied to a new field in a dissipative

dynamic system to find a stable region in the system^[30–32]. On the other hand, the dynamic stabilization mechanism based on the phase control was proposed and applied to the stabilization of plasma instabilities including the RTI, the filamentation instability, and also the fuel target implosion in heavy ion inertial fusion (HIF)^[20, 22, 23, 29]. Originally the dynamic stabilization mechanism comes from the imperfect feedback control, which is widely used to stabilize tall buildings, structures, etc. in our society. In the perfect feedback control, the displacement and its phase are measured, and the additional perturbation is added to stabilize the systems. In plasmas we cannot measure the perturbation phase and amplitude. As we discussed in this paper, we can actively apply the perturbations. Before moving to the system disruption or before developing the nonlinear phase, the additional perturbations, which should have the reverse phase, are applied actively, and then the superimposed total amplitude could be mitigated.

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