# SIMULATED GLACIER SLIDING OVER AN OBSTACLE

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ABSTRACT. The sliding of temperate ice over two obstacles with sine-wave profiles (wavelength, 0.53 m; maximum slope, 0.22) and low thermal conductivity has been reproduced at full scale within a steel chamber. As expected, large cavities form between the ice and the obstacles so that the drag is limited. However, the delayed elasticity of bubbly ice modifies the expected behaviour. At the base of the ice a fine-grained, bubble-free blue ice layer develops. The shear strain concentrates on the up-stream side of bumps and in the blue ice layer. Tap-water ions enhance tertiary creep-rates.

Résumé. Simulation du glissement d'un glacier sur une bosse. On a reproduit le glissement d'un glacier tempéré sur deux bosses (longueur d'onde, 0,53 m; pente maximale, 0,22) en vraie grandeur dans une chambre d'acier. Il se forme vraiment de grandes cavités, qui empêchent le frottement de s'élever, mais l'élasticité différée de la glace bubeuse modifie le comportement auquel on s'attendait. A la base se développe une couche de glace bleue, sans bulles et à grains fins. Le cisaillement se concentre sur la face amont des bosses et dans la couche de glace bleue. Les ions de l'eau de ville favorisent le fluage tertiaire.

ZUSAMMENFASSUNG. Simulation des Gletschergleitens über einen Buckel. Das Gleiten eines temperierten Gletschers über zwei Buckel (Wellenlänge, 0,53 m; maximales Gefälle, 0,22) wurde im Originalmassstab innerhalb einer Stahlkammer nachgebildet. Es bilden sich tatsächlich grosse Hohlräume, die ein Anwachsen des Zugwiderstandes verhindern, doch verändert die verzögerte Elastizität blasenreichen Eises das erwartete Verhalten. An der Unterseite entwickelt sich eine Schicht feinkörnigen, blasenfreien Blaueises. Die Scherspannung konzentriert sich auf die stromaufwärts gelegene Seite der Buckel in der Blaueisschicht. Die Ionen des Leitungswasser begünstigen tertiäres Kriechen.

#### INTRODUCTION

The idea of reproducing in the laboratory the conditions which exist at the ice-bedrock interface originated in February 1962 during a seminar given by Professor L. Lliboutry on the theory of glacier sliding. He showed that the laws describing permanent and transient creep in ice were ill-defined, calculations relating to the creep were in their infancy, and important processes had not been considered. The complexity of the creep law made it difficult to change the time scale and, since at least two other parameters were important, the machine had to be designed on a large scale. The technological problems looked formidable, but this was an inducement to carry out the work. A viscometer named "Penelope", was constructed in 1964 and modified several times between 1966 and 1977.

In spite of its imperfections, the viscometer has enabled deep insight to be made into the processes occurring at the ice-rock interface. In the meantime, sliding theory has been considerably improved (Lliboutry, 1968; Nye, 1969; Kamb, 1970). Thus, the experiments carried out using Penelope are now quantitative. Strain-rates around a bump can be measured in order to check the assumptions of sliding theories.

# DESCRIPTION OF THE VISCOMETER

#### Mechanical details

Since a linear machine would have to be prohibitively long to be able to reach a steady state, a circular design similar to that of a large Couette viscometer was preferred (Fig. 1). The outer, moving part consists of two steel hemispheres (1-2), with a steel annulus between them. On the inside of this annulus, another annulus made of plastic-impregnated wood (3) is fastened. This has 20 cogs which pull a circle of ice around, simulating the drag of basal ice by a glacier. The arrangement is secured by threaded bolts and nuts (9). This almost spherical enclosure of about 0.60 m diameter can withstand a pressure of 100 bar.

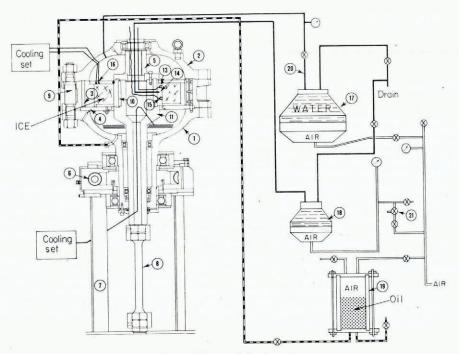


Fig. 1. Diagram of the viscometer.

A cog wheel moved by a worm gear (6) is driven by an electrical motor through two gearboxes and a speed reducer. A drum made of moulded plastic (10) with diametricallyopposite raised obstacles simulates the bedrock, it is attached to a stationary steel hub (10). The hub transmits the torque to a calibrated steel rod (8); the opposing torques on this rod and on the worm gear balance through the U-shaped supports (7). At its upper end the hub is fastened to a flared hollow column (5) which centres the upper surface.

Between the toothed annulus and the drum an ice ring is formed. Its dimensions are given in Figure 2. When the machine operates the flow is two-dimensional and the sliding on the cogs (principally by melting-refreezing) is negligible. The velocity on the bumps is 100 m/year if the mobile enclosure makes one revolution in 98.5 h. Experiments were made with velocities in the range 60-1 000 m/year.

## Pressure control

The pressurized enclosure is divided into two chambers by a base (4). The upper chamber is filled with water, the lower one with oil. The same pressure, provided by a nitrogen cylinder, is applied to the water through (17) and to the oil through (19). This arrangement was designed because the viscometer was not originally in a cold room. At that time the oil chamber was cooled and the machine was insulated with a polyurethane jacket. The main difficulties were that it was impossible to remove the ice from the viscometer at the end of an experiment, because of the delayed elastic response of bubbly ice. It was also difficult to keep both sides of the ice watertight, in order to allow the water pressure in the cavities to be independent of the confining pressure. Further, it was difficult to maintain the ice at the melting-point for a long time with only negligible melting. This problem was solved when a new building for the Laboratoire de Glaciologie was constructed in 1973. Today, with the

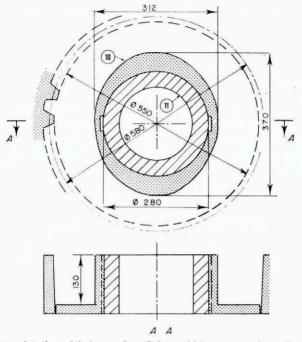


Fig. 2. The drum with its two obstacles and the ice annulus. Only two driving cogs are shown, there are 20 in all. Dimensions in millimetres.

viscometer in a room at  $0 \pm 1^{\circ}$ C, this cooling device is used only for making the ice ring and for adjusting the temperature exactly to the melting-point at the experimental pressure.

The pressure in the cavities at the lee of the obstacles is recorded with the pressure gauge (13), and may, at the moment, be fixed independently through the pressure intake (14) and the pressure flask (18), but when the experiments reported here were made there were only two alternative configurations:

- (i) closed tap; the pressure in the cavities adjusts itself according to the velocity, the confining pressure, and the size of the cavities (Lliboutry's *autonomous regime*);
- (ii) open tap; the pressure in the cavities is atmospheric (Lliboutry's interconnected regime).

Nevertheless, by starting with the tap closed and then letting a few cubic centimetres of water flow out through the tap, the pressure in the cavities could be modified for some hours. In this way, for given values of velocity and confining pressure, several values for the cavity pressure were obtained with the same ice specimen.

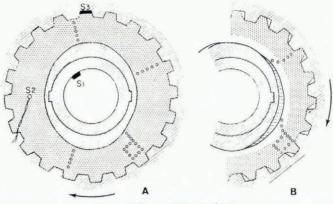
As already mentioned, it was very difficult to keep the interface between the plastic drum and the ice watertight. In the original drum, the surfaces were marked with concentric circular grooves, but this drum consisted of four sections and two obstacles fastened together. Some regelation ice formed in the joints and progressively separated the sections (an undesirable glacial quarrying of the bedrock had been simulated). Subsequently, the two obstacles were rigidly fastened to the circular sectors. The drum now in use is moulded as a single unit. The solution for the lower surface was to produce a very slight local freezing using the cooled oil chamber. For the upper surface, the answer was to allow the cheek to move with the ice (an O-ring being incorporated at the junction). Nevertheless, in order to

#### JOURNAL OF GLACIOLOGY

keep the upper cheek reliably watertight, a slight refreezing along the ring (16) has been used since 1977. The refrigeration comes from another cooling system which moves with the steel enclosure.

#### Temperature control

Temperature control was difficult until the viscometer was set up in a room at  $0^{\circ}$ C. Three thermistors were originally provided (Fig. 3): one inside the hub (s1), another within the ice (s2), and a third on the driving cogs (s3). The first thermistor, since it had a much faster response to changes in the cooling-rate, was used for temperature regulation. In the present version of the viscometer, the thermistors on the obstacles (Fig. 4) achieve an adequate temperature control. The temperature variations on the up-stream side of the bumps are recorded in the most recent tests, the temperature response is almost instantaneous.



#### Fig. 3. February 1973 experiment.

A. The appearance of the marks before deformation.

B. Subsequent appearance of the marks after 5.05 revolutions.

There is significant deformation in the "basal" layer.

## CAVITY FORMATION AND TORQUE MEASUREMENTS

#### Formation of cavities

The upper hemisphere is now fitted with observation ports for the observation of the ice, but ice modifications were originally observed by releasing the confining pressure and opening the chamber.

The ice annulus is made by soaking crushed ice with melt water from similar ice (or tap water in the case of commercial ice), and cooling the mixture. Air bubbles cannot be completely eliminated, and the normal density of this artificial, isotropic ice is about 0.86 Mg/m<sup>3</sup>.

There was originally a large gap between the upper surface of the drum and the driving cogs in order to allow ice to flow outwards during the formation of the cavities. This process has not, in fact, been observed, probably because bubbly ice is compressible. Under the pressure of several tens of bars, generated at the up-stream surface of the obstacles, the bubbly ice contracts by about 4% by collapse of the air bubbles. Bubbly ice behaves as a viscoelastic material, with a large delayed elasticity. Thus, on the down-stream side of the bumps there is no immediate elastic rebound, and cavities are formed from the beginning of the experiment. They grow a good deal during the first half revolution, and very slowly after this.

# SIMULATED GLACIER SLIDING

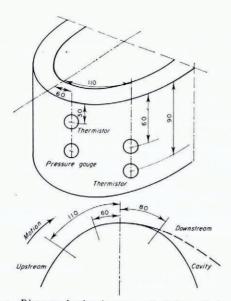


Fig. 4. Diagram showing the sensors attached to each obstacle.

Consequences of this are: (1) a large torque is measured even when both the confining pressure and the pressure in the cavities are at atmospheric pressure; (2) at the beginning of the experiment, when the cavities are not yet formed, the torque does not rise to very high values, even with high sliding velocities. The torque will be expressed as a mean drag over the "bedrock"  $\tau_{\rm b}$ .  $\tau_{\rm b}$  is always less than 3 bar, even for a sliding velocity U of 145 m/year.

A new drum with larger cheeks was constructed after the discovery of this unexpected behaviour. This increase in size does not allow any ice outflow, but does permit any water at the working pressure to penetrate between the ice annulus and the driving cogs. Of course, there is a danger that, if the bubbly ice is not compressible enough to allow the formation of large cavities, the mean pressure within the ice ring will rise well above the confining pressure. This is prevented by allowing the ice annulus to melt very slowly (rather than freeze very slowly by cooling too strongly). This is a makeshift arrangement which makes very accurate and continuous control necessary. In Penelope's successor (a new machine called Telemachus) a much better solution has been adopted; the confining pressure is obtained by squeezing the ice with a ram coupled to a hydraulic jack.

# Variation of the drag with time

Surprisingly, the variations in the torque when the machine starts are almost independent of the size of the cavities. Figure 5 is an example of this behaviour, it refers to an experiment of May 1970, with a sliding velocity U = 111 m/year, in the autonomous regime, using ice frozen from tap water. There was no confining pressure, but the mean pressure in the ice was certainly higher than atmospheric.

At time t = 0, the machine was started, at this stage cavities are not present. The rapid increase in the drag should be governed by the elasticity of bubbly ice (the machine is stiff enough to make its elastic deformation almost negligible). At t = 16.5 h (0.188 revolution) and 51.5 h (0.586 revolution) the machine was stopped; the drag was observed to fall exponentially, this shows the delayed elasticity. When the machine was set in motion again there was:

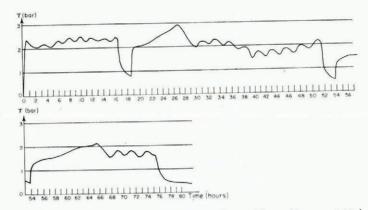


Fig. 5. Variations of the drag with time during the May 1970 experiment. The machine was stopped at 17 h and 51 h for about two hours so that the deformation of the frames could be observed.

- (1) a sudden increase of the drag (up to  $\tau_b = 2$  bar the first time, up to 1 bar the second time, when the cavities are larger);
- (2) a progressive increase by a further bar more in about 10 h (the sliding during this time is about 12 cm);
- (3) a lowering by almost the same amount and then regular oscillations with a period of about 140 min (corresponding to 2.0 cm of sliding).

These slow, regular oscillations have been observed in all the experiments. They neither correspond to the periodicity of the cogs (which, reduced to the "bedrock" is 5.36 cm) nor to any periodicity in the temperature-monitoring system. The relaxation time of the viscoelastic ice has been found to be of the order of minutes, not of hours. These drag oscillations at constant velocity may be the same phenomenon as the fluctuations in strain-rate observed by Duval (1976, in press) during tertiary creep under a constant load. He attributes the strain-rate fluctuations to successive periods of prevailing strain-hardening and recrystallization. The larger preliminary drag, without fluctuations, would then correspond to transient and secondary creep. Nevertheless, these oscillations almost disappeared when the initial bumps were changed. The first ones did not have an exact sine profile, being steeper at their ends (Fig. 6). So, these oscillations may be alternatively related to some process of periodic microfracturing as has already been introduced by Michel (1978).

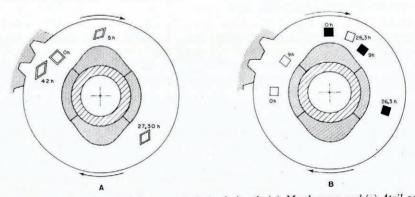


Fig. 6. Diagrams showing the motion of the frames put in the ice during the (A) March 1970, and (B) April 1970 experiment.

# Estimation of the real pressure within the ice

As already explained, we can have no confidence that the mean pressure in ice  $p_i$  (which simulates the glacier weight) equals the confining water pressure  $p_c$ . Nevertheless, this important parameter has been estimated by the following procedure:

If the pressure in the cavities is suddenly changed by  $-\Delta p$  (the length of the cavities having no time to change), the change of the drag  $\Delta \tau_b$  is the same as if the pressure of ice against the up-stream side of the obstacles had been increased by  $\Delta p$ . Following Lliboutry's notation (Lliboutry, 1975) let  $\mathcal{N} = p_1 - p$  be Terzaghi's effective pressure and s the ratio of the area in contact to the total area of the "bedrock". The mean pressure of ice against the obstacle where there is contact is  $\mathcal{N}/s$ . Since it has been shown in many experiments that  $\Delta \tau_b$  is exactly proportional to  $\Delta p$ , we assume that the same ratio exists between  $\tau_b$  and  $\mathcal{N}/s$ . It is then sufficient to measure  $\tau_b$ ,  $\Delta \tau_b/\Delta p$ , and s to obtain  $\mathcal{N}$ .

For example, during the experiment of February 1973, with U = 208 m/year,  $\Delta \tau_b/\Delta p = 0.066 \pm 0.001$ . Since  $\tau_b = 3.7$  bar,

$$\frac{\mathcal{N}}{s} = \frac{3 \cdot 7}{0.066} = 56 \text{ bar.}$$

Now the length of ice in contact with each obstacle was  $9.0 \pm 0.2$  cm, and since  $\lambda = 53.6$  cm, s = 9.0/53.6 = 0.17, and thus N = 9.5 bar. During this experiment p = 0 and  $p_c = 5$  bar, relative to atmospheric pressure. If we had assumed  $p_i = p_c$ , we should have obtained the incorrect value for N of 5 bar. Nevertheless, this estimation is still not entirely accurate because s changes progressively when p is altered. For this reason, and because it has not been possible until recently to maintain pressure values steady for several weeks, we cannot give any law for  $\tau_b(N)$  at the moment.

#### ICE PETROLOGY

The thermal conductivity of "Afcodur-PVC" (1.6 kJ/m/deg/h) is of the same order of magnitude as that of rock (e.g. 3.6 kJ/m/deg/h for limestone). Some regelation ice is found in the cavities, near the point where the ice annulus separates from the "bedrock". Nevertheless, as will be shown in the next section, most of the sliding comes from plastic deformation. This is consistent with the theory without cavitation, which indicates that

$$U_{\mathbf{p}}/U_{\mathbf{f}} = (\lambda/\lambda_{\mathbf{x}})^2,$$

where  $U_p$  is the plastic sliding contribution,  $U_f$  is the contribution to sliding made by the melting-refreezing process, and  $\lambda_{\star}$  is the transition wavelength. The latter is estimated by Lliboutry (1975), in the metre-bar-year unit system, as

$$\lambda_{\mathbf{x}} = 0.63 (U\tau_{\mathbf{b}})^{-\frac{1}{2}}.$$

In all our experiments U > 60 m/year and  $\tau_b > 1 \text{ bar}$ , whence  $\lambda_{\star} < 0.16 \text{ m}$ . Since  $\lambda = 0.536 \text{ m}$ , we have  $U_p/U_f > 11$ .

After 1.5 revolutions the ice nearest to the hub becomes slightly clearer. After 8.5 revolutions a layer of blue, perfectly bubble-free ice, 3 cm thick, has been formed. We shall see that this "basal" ice close to the obstacles and the cavities has been deformed the most. It is not regelation ice because small geometric figures marked in the ice during experiments become deformed but do not disappear (Fig. 3). The ice crystals are very minute (about 1 mm<sup>2</sup> in cross-sectional area, as measured on thin sections), and the air bubbles have been expelled into the cavities, where the pressure is less. Merrill (1960) has already observed a slow migration of bubbles near a sampling hole dug in the wall of a tunnel in cold ice. With temperate ice, large strain-rates, and a strong recrystallization the expulsion of air bubbles is much faster.

#### JOURNAL OF GLACIOLOGY

A strong ice fabric develops during the experiments which is similar to one observed in glaciers (Rigsby, 1960; Vallon and others, 1976). It is very well developed in the blue ice. A stereogram is given (Fig. 7). The *c*-axes cluster in a girdle with four maxima, two of the maxima (with 25% of the crystals in each one) point laterally at about  $45^\circ$  from the plane of symmetry, another (15% of the population) points backwards (when seen from above, i.e. from the driving cogs towards the hub), the fourth maximum points forward. This ice fabric, already observed in glaciers, was reproduced for the first time in our laboratory, in 1968 using Penelope. Since then Duval (1976, in press) has shown that this ice fabric always forms by syntectonic (parakinematic) recrystallization when the state of strain is not simple shear.

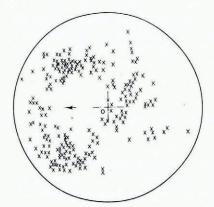


Fig. 7. Ice fabric formed in blue ice.

#### **OBSERVED STRAINS**

### First rough technique

The first method used to observe strains was to put a square frame  $(47 \times 47 \text{ mm}^2)$  within the ice in a plane perpendicular to the axis of the machine with two sides parallel to the "bedrock" (the circumference of the drum). The sides of the frame were 5 mm thick, and saw-cuts were made at the four corners to allow it to deform to a rhombus. Successive positions of the frames are shown in Figure 6. The deviations of these frame angles from  $\pi/2$ are given in Table I. In both experiments the ice was made with tap water. Deformation occurred whilst the frame was moving along the up-stream side of the obstacle. There was no significant deformation after this until the second obstacle was reached, only rotation occurred, with the "upper side" moving faster. The deformation over the second obstacle was less, probably because the rhombus no longer had two sides parallel to the "bedrock".

# TABLE I. DEVIATIONS OF THE FRAME ANGLES FROM $\pi/2$ rad

	Sliding velocity m/year	Time h	Frame angles rad
Experiment A (Fig. 6A)	425 425	5 27	$0.26 \pm 0.04$ $0.29 \pm 0.04$
	425	42	0.47±0.03
Experiment B (Fig. 6B)	111	9	$0.007 \pm 0.001^* 0.065 \pm 0.015^{\dagger}$
	111	26.3	0.132±0.003* 0.053±0.013†

\* Shown as a clear square in Figure 6B.

† Shown as a dotted square in Figure 6B.

#### SIMULATED GLACIER SLIDING

In Experiment B, when passing over the first three-quarters of a bump, the clear frame (Fig. 6) was deformed by 0.125 rad. When passing over the second half of an obstacle, the dotted frame was deformed by 0.065 rad. Thus, on this occasion, the deformation went on in the same direction over the down-stream side of the obstacle. Over the whole bump it was about 0.16 rad instead of 0.29 rad as in Experiment A. Rotation was negligible in B.

## Explanation of the results

The only simple analytical solution with which these results may be compared is that for the case of no cavitation, infinitesimal slopes, and Newtonian viscous ice. These assumptions are so far from the truth that we may assume without inconvenience that the ice slides over a sine curve  $z = a \cos \omega x$  from  $x = -\infty$  to  $+\infty$  instead of considering circular sliding where  $r = r_0 + a \cos \omega \theta$ . It can be shown that the variations in pressure over the driving cogs ( $\omega z = 1.4$ ) are 3.019 times larger than for a semi-infinite solid (Appendix). On the bumps (z = 0) the pressure variations are 2.443 times larger, the same applies for the drag which is

$$\tau_{\rm b}=2.443\eta Ua^2\omega^3.$$

The frames were put midway between the cogs and the bumps ( $\omega z = 0.7$ ). If cavitation does not occur in the Newtonian-viscous case, the total rotations on the up-stream side of a bump should be  $\Omega = -0.008$  rad and the shear deformation  $\epsilon_{xz}$  should equal -0.072. This is not the case in our experiments, because the general shear caused by the drag has been ignored. This shear for a full wavelength is

$$\begin{array}{l} \gamma_{\rm b} = 2.443 U a^2 \omega^3 T = 2.443 a^2 \omega^3 \lambda \\ = 2.443 \times 2\pi a^2 \omega^2 = 0.443 \ 6. \end{array}$$

The experiments show that, in the case of cavitation, most of this shear concentrates over the area where ice and bedrock are in contact, the more so as the sliding velocity increases.

Much more precise numerical computations are in progress, using the finite-difference method and the finite-element method. They will be published elsewhere.

# A more accurate technique for the measurement of strain

In order to measure the normal strains as well as the angular deformations, small plastic markers were put within the ice, along different radii, numbered o to 19. One layer J was 5 cm from the lower side, another layer R at 4 cm from the upper side. Their motion was identical, indicating that the flow was effectively two-dimensional. Only a few marker positions are indicated on Figure 8. In this figure, A indicates the starting point and p the

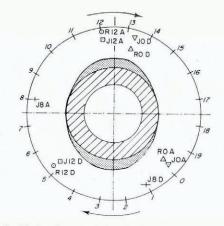


Fig. 8. Motion of marks during the January 1973 experiment.

end point. The position of the marks was accurately determined by measuring their distance to several driving cogs.

# Experiment of January 1973 (tap-water ice)

Only 1.323 revolutions were carried out at a sliding velocity of 145 m/year. The experiment was so short that blue ice did not form. The results are plotted in Figure 9. The markers which were on the same radius remained in a straight line. For the marks R0 and J0, which passed over two obstacles, the total angular deviation was  $0.211\pm0.012$  rad. For the marks J8, R12, and J12, which passed over three obstacles, the deviation was  $0.476\pm0.023$  rad. It may be that during the first traverses over the obstacles the cavities were not yet well developed and the strain was less concentrated. The ice crystals, although still not very large, were of a significant size after 80 h (Fig. 10).

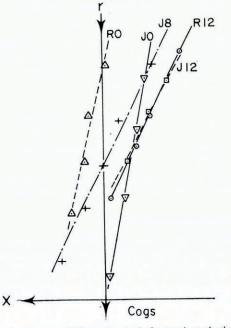


Fig. 9. The observed shear after 1.323 revolutions at a speed of 145 m/year in the January 1973 experiment.



Fig. 10. Ice fabric from the January 1973 experiment; tap-water ice deformed for 80 h.

## Experiment of February 1973 (tap-water ice)

The velocity was 143 m/year for the first 1.3 revolutions and subsequently 208 m/year. The markers were placed as indicated on Figure 3A. After 5.05 revolutions lasting 270 h the situation was as shown in Figures 3B and 11. A bottom layer of blue ice, 2 cm thick, formed where the shear strain was strongest ( $\gamma_{xz} \approx 0.83$ ). Above it, in the bubbly layer, the square of  $47 \times 47$  mm<sup>2</sup> became a rectangle of  $53 \times 40$  mm<sup>2</sup>. Final values for the strain are

$$\begin{aligned} \gamma_{xz} &= 0.13 \pm 0.03, \\ \epsilon_{xx} &= 0.12, \end{aligned}$$

and

$$6 = -0.16$$

The density of the bubbly ice has thus increased by 4% (0.860 to 0.895 Mg/m<sup>3</sup>). Figure 13 shows crystals with very fine grain size in the boundary layer of the blue ice.

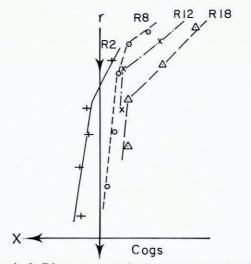


Fig. 11. Observed shear in the February 1973 experiment; tap-water ice deformed by 5.05 revolutions.



Fig. 12. Ice fabric from the February 1973 experiment; tap-water ice deformed for 200 h.

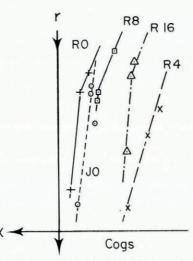


Fig. 13. Observed shear in the April 1973 experiment; distilled-water ice deformed by 5.30 revolutions.



Fig. 14. Ice fabric from the April 1973 experiment; distilled-water ice deformed for 365 h.

#### Experiment of April 1973

The velocity in this experiment was 143 m/year for a total duration of 365 h (5.30 revolutions). On this occasion the ice was made from distilled water instead of the tap water used in previous experiments. The same layer of blue ice about 3 cm thick was formed, but within it the shear strain was substantially less, as shown in Figure 14. On the other hand,  $\tau_b$  was 1.66 times higher. Figure 14 shows the much larger blue-ice crystals which are obtained with distilled water. This indicates that the ions present in tap water enhance ice recrystallization and creep.

#### CONCLUSIONS

Although they have certain errors, the experiments carried out in 1970 and 1973 with the viscometer indicate that important facts are ignored in the present theories. The delayed elasticity of bubbly ice, which is much more important than the pseudo-elasticity of Duval ([1977]) and which is of the Kelvin not of the Maxwell type, cannot be ignored; it increases the drag. The progressive elimination of air bubbles from the bottom ice of glaciers would appear to be an important process. A better simulation of sliding processes would occur if bubble-free ice were used. Kamb's (1970) statement that the layer of blue ice found at the bottom of glaciers is caused by regelation may be questioned; in the ice tested here it is not the case. This is consistent with the findings of Souchez and others (1978) who have shown that the ionic composition of base glacier ice cannot arise as a result of a classical meltingrefreezing process.

Creep-rates in ice are considerably altered by the presence of ions. This makes it very difficult to reproduce the exact mode of basal deformation over an obstacle. At best we may determine the friction law over a sine profile for different known ionic contents.

A new viscometer, a development of Penelope, is now ready to work in Grenoble. Nevertheless, Penelope will still be useful because the flow in it is two-dimensional and very high confining pressures can be attained; this will not be possible with the new viscometer.

## ACKNOWLEDGEMENTS

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## APPENDIX

The profile of the "bedrock" is given by

 $* = a \cos \omega x$ .

the boundary conditions are

for z = h, (1) forward velocity u = U, a constant;

(2) transverse velocity w = 0;

for  $z \approx 0$ ,

(3) shear strain-rate

$$\dot{\gamma}_{xz} = \frac{\partial u}{\partial z} + \frac{\partial w}{\partial x} = 0;$$

(4) to second order, q(x, z) denotes the strain function, q = 0 gives  $z = a \cos \omega x$ . A general solution of the biharmonic equation  $\nabla^4 q = 0$  is

$$= f(z) \cos \omega x + g(z) \sin \omega x + C_1 z + C_2 z^2 + C_3 z^3,$$

f(z) and g(z) being of the form  $(A + B\omega z) \exp(\omega z) + (C + D\omega z) \exp(-\omega z)$ . The boundary conditions are then  $f'(h) = 0, \quad g'(h) = 0,$ (1)

$$\hat{C}_1 + 2C_2\hat{h} + 3C_3\hat{h}^2 = U,$$

$$f(h) = 0, g(h) = 0, f''(0) + \omega^2 f(0) = 0, g''(0) + \omega^2 g(0) =$$

$$C_2 = 0,$$
  
f(0) =  $-Ua,$  g(0) = 0.

The four relations

$$g(h) = g'(h) = g(o) = g''(o) = o$$

imply that g(z) = 0. In order not to have a constant term for

$$\frac{\partial \sigma_x}{\partial x} = -\frac{\partial \tau_{xz}}{\partial z},$$

 $C_3 = 0$  is needed.

Hence,

(2

(4)

$$\left. \begin{array}{ccc} C = -A - Ua, & D = B - Ua, \\ A \left( \exp\left(2\omega h\right) - 1 \right) + B\omega h \left( \exp\left(2\omega h\right) + 1 \right) = Ua(1 + \omega h), \\ 2A \exp\left(2\omega h\right) + B\left[ \left(1 + 2\omega h\right) \exp\left(2\omega h\right) + 1 \right] = Ua. \end{array} \right\}$$
(A-1)

In our case, h = 0.12 m and  $\omega h = 1.4$ . Finally,

$$u = [U + Ua\omega^2 z \exp(-\omega z) \cos \omega x] + Ua\omega(0.727 \cosh \omega z - 0.716\omega z \sinh \omega z) \cos \omega x$$

the terms in square brackets are the solution for  $h = \infty$ . With a uniform velocity at a finite distance the modification is not negligible, in particular, against the "bedrock" the forward velocity u increases over the bump. The normal stress  $\sigma_z$  is calculated as

$$\frac{\partial \sigma_z}{\partial z} = -\eta \left( 3 \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial z^2} \right). \tag{A-3}$$

It yields

 $\sigma_{z} = \left[-p_{i}+2\eta U a \omega^{2}(1+\omega z) \exp\left(-\omega z\right) \sin \omega x\right] +$ 

 $+2\eta Ua\omega^2(1.443 \cosh \omega z - 0.716\omega z \sinh \omega z) \sin \omega z$ (A-4)

$$\int_{-T/2}^{0} \frac{\partial u}{\partial z} dt = \int_{-\lambda/2}^{0} \frac{\partial u}{\partial z} \frac{dx}{U} = [-0.471 \ 8a\omega \sin \omega z]^{\circ}_{-\lambda/2} = -0.080,$$
$$\int_{-T/2}^{0} \frac{\partial w}{\partial x} dt = \left[\frac{w}{U}\right]^{\circ}_{-\lambda/2} = [-0.378 \ 65a\omega \sin \omega x]^{\circ}_{-\lambda/2} = -0.054.$$

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