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A THEOREM IN THE PARTITION CALCULUS CORRIGENDUM

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We are grateful to Dr. A. Kruse for drawing our attention to some misprints in [1], and also to a technical error in our deduction of (19) which we remedy below.

Misprints. 1. Page 502, last line. Replace ω^{12} by ω^{11}.
2. Page 505, equation (17). This should read:

$$g_i(g_{i+1}(\cdots(g_{j-1}(\gamma_i))\cdots)) = \gamma_i \qquad (i < j < \omega). \tag{17}$$

3. Page 505, line 3. Replace (12) by (14).
4. Page 505, line 4. The displayed formula should read

$$\rho = g_i(g_{i+1}(\cdots g_{j-1}(\gamma_j))\cdots).$$

In order to make (19) correct we define x_n, $S^{(n)}(n<\omega)$ a little more carefully and replace lines 21–31 on Page 504 by the following:

Let $n<\omega$ and suppose that we have already chosen elements $x_i \in S$ $(i<n)$ and a subset

$$S^{(n)} = \bigcup (\nu \in B) A_\nu^{(n)}(<) \tag{12}$$

of S of order type $\alpha\beta$ such that $S^{(n)} \subset K_1(\{x_i : i<n\})$. If $\alpha \geq \alpha+\alpha$, then choose sets $A, A' \subset A_{\gamma_n}^{(n)}$ such that $A<A'$; if on the other hand $\alpha \ngeq \alpha+\alpha$, then put $A=A'=A_{\gamma_n}^{(n)}$. In either case it is true that if $x \in A$ and $A_1' \subset A'$, then there is $A_2' \subset A_1$ such that $\{x\}<A_2'$. With this remark in mind, it now follows from (10) that there are $x_n \in A$, a strictly increasing map $g_n : B \to B$ and sets $A_\nu^{(n+1)}$ $(\nu \in B)$ such that

$$g_n(\gamma_i) = \gamma_i \qquad (i \leq n), \tag{13}$$

$$A_\nu^{(n+1)} \subset K_1(x_n) \cap A_{g_n(\nu)}^{(n)} \qquad (\nu \in B), \tag{14}$$

$$\{x_n\} < A_{\gamma_n}^{(n+1)} \subset A'. \tag{16}$$

From the definition of A, we also have

$$x_n \in A_{\gamma_n}^{(n)} \subset S^{(n)}. \tag{15}$$

Reference

1. P. Erdös and E. C. Milner, *A theorem in the partition calculus*, The Canadian Mathematical Bulletin, **15** (1972), 501–505.